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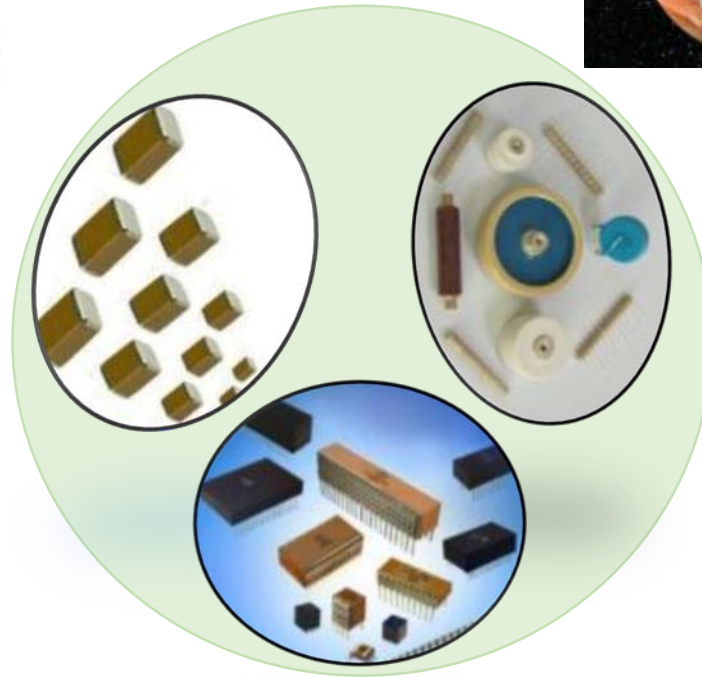
Grain-size-dependent dielectric properties in nanograin ferroelectrics

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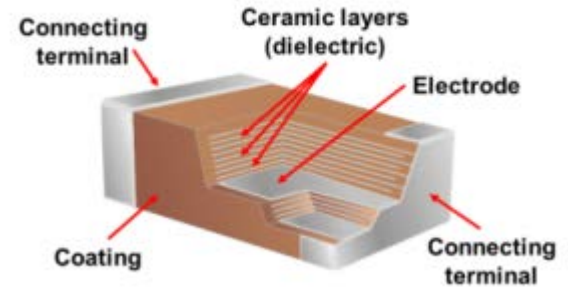
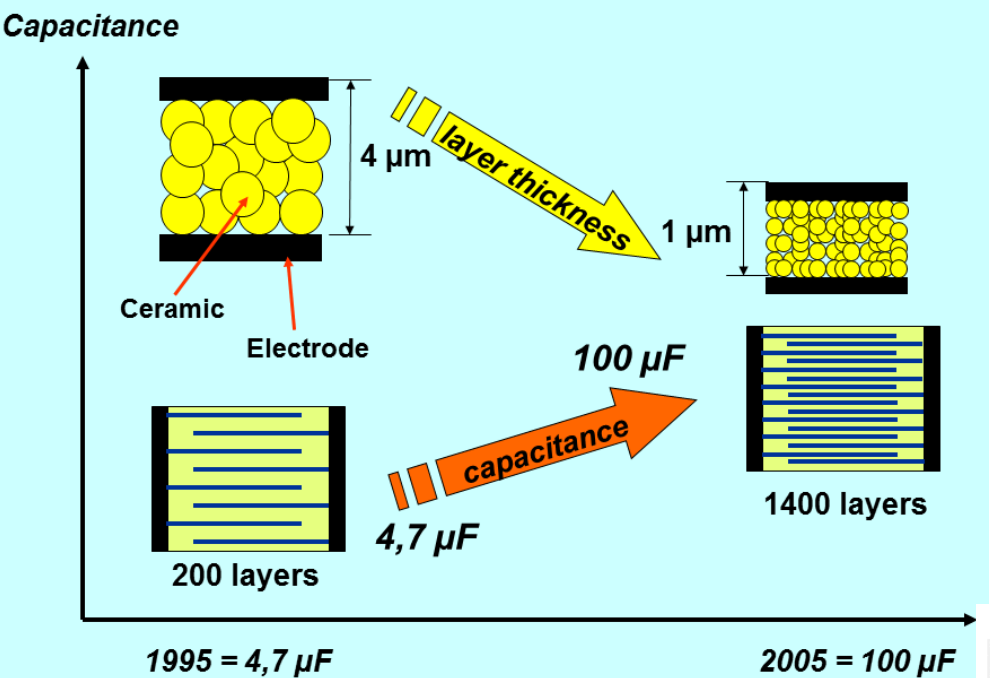


Application of ferroelectric capacitors

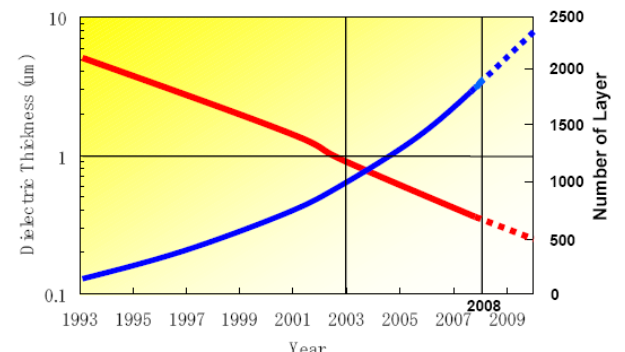
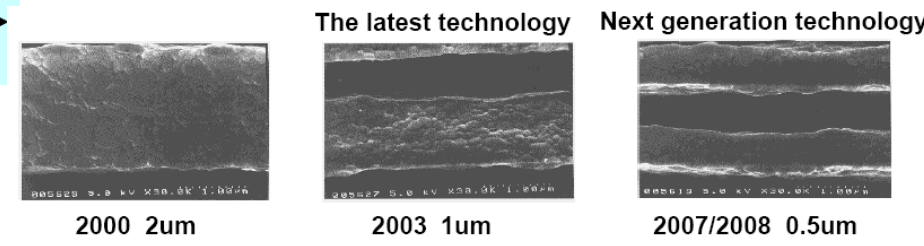
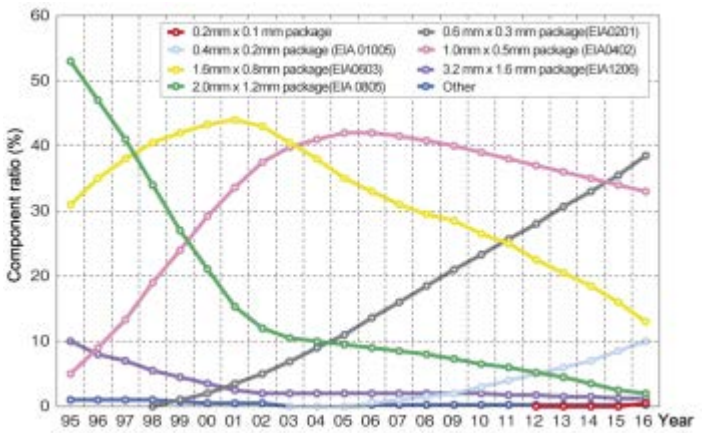




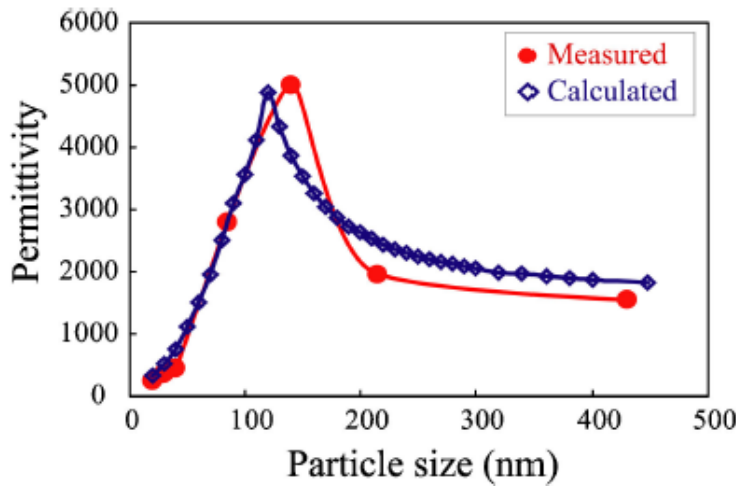
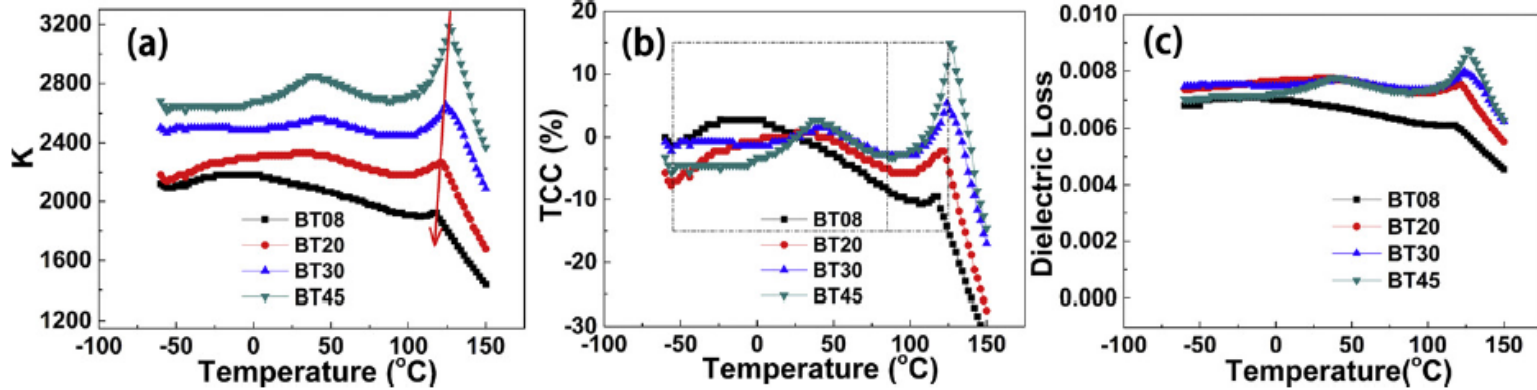
Miniaturization of ferroelectric capacitors



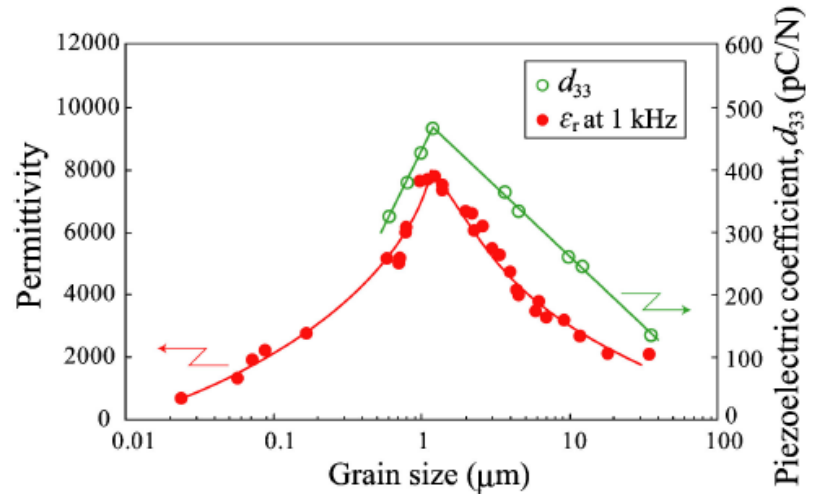
$$C_{MLCC} = C_1 + C_2 + C_3 + C_4 + \dots + C_{n-1}$$



Size effect in ferroelectrics



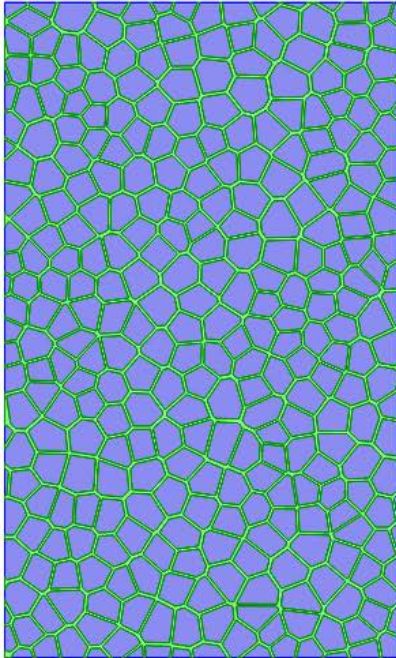
BaTiO₃ powders



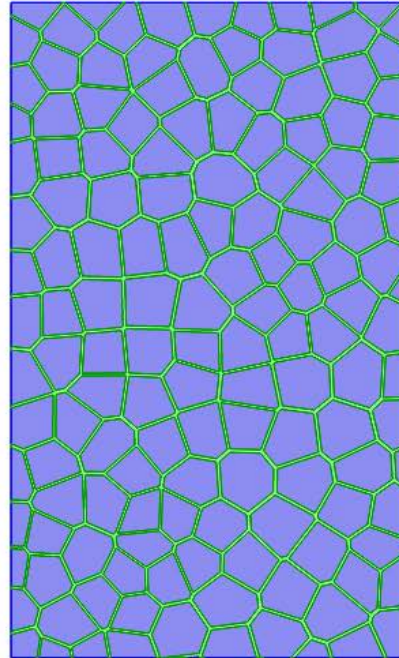
BaTiO₃ ceramics

[1]H. Gong, X. Wang, S. Zhang, H. Wen, L. Li, *Journal of the European Ceramic Society* 2014, 34, 1733.
 [2]T. Hoshina, *Journal of the Ceramic Society of Japan* 2013, 121, 156.

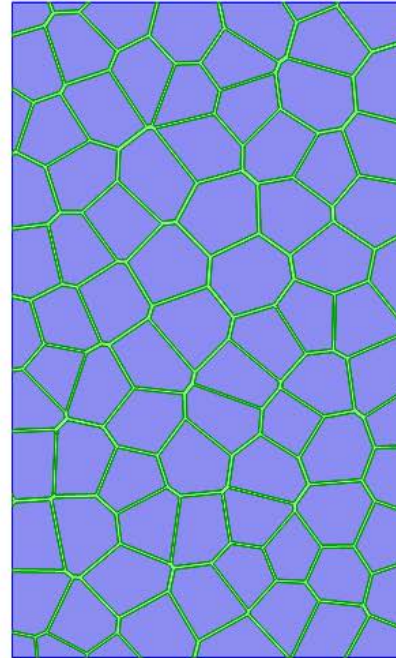
Grains: Voronoi polygonal



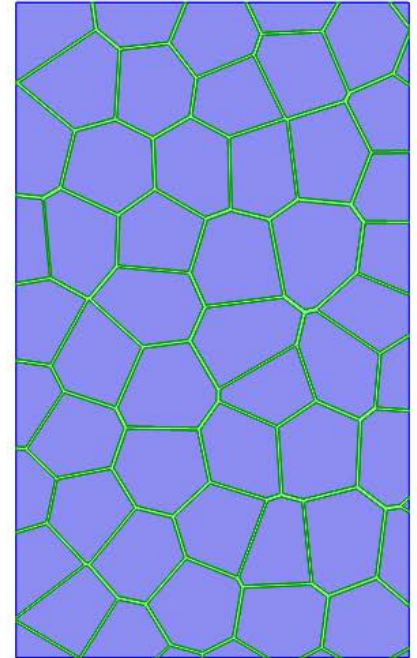
50nm



75nm



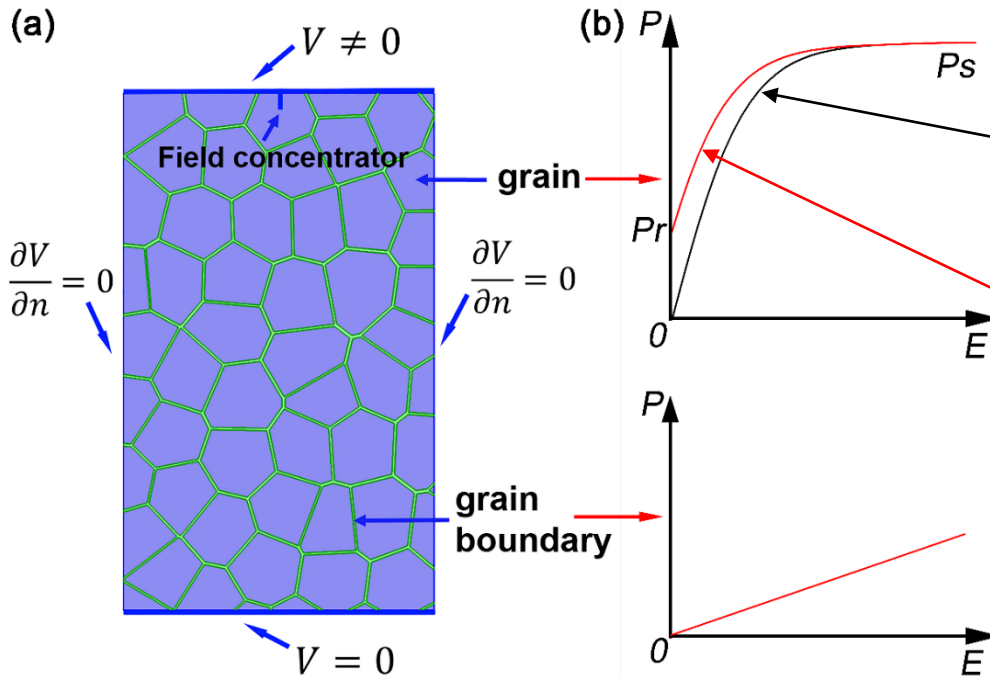
100nm



125nm



Modeling process



Modified hyperbolic tangent model on electric hysteresis:

1) Charge process (down branch)

$$P = P_s \tanh \left[\frac{\varepsilon_0 (\varepsilon_g(0) - 1) E}{P_s} \right]$$

$$\varepsilon'_c = 1 + \frac{P_s}{\varepsilon_0 E} \tanh \left[\frac{\varepsilon_0 (\varepsilon_g(0) - 1) E}{P_s} \right]$$

2) Discharge process (up branch)

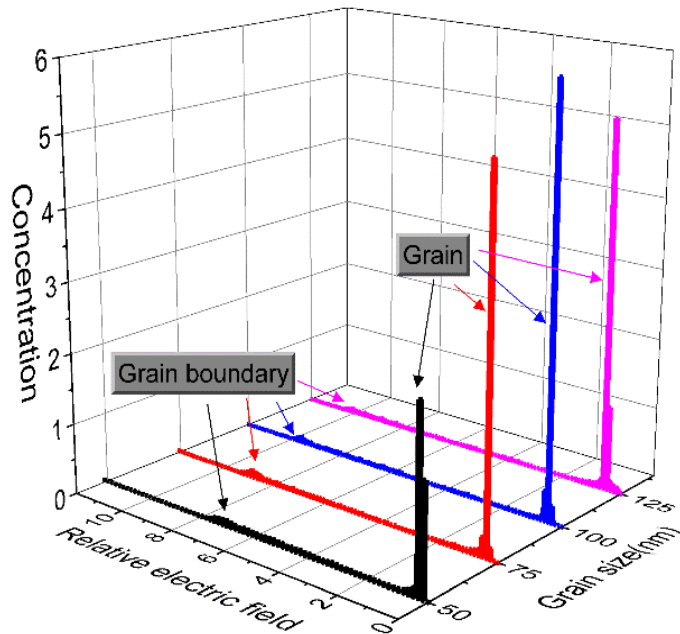
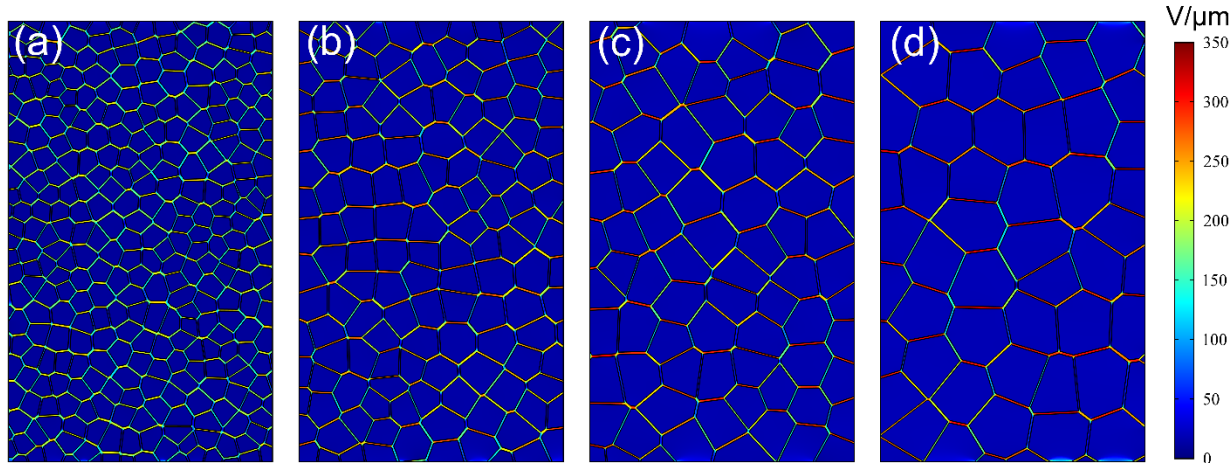
$$P = P_s \tanh \left[\frac{\varepsilon_0 (\varepsilon_g(0) - 1) (E + E_c)}{P_s} \right]$$

$$\varepsilon'_c = 1 + \frac{1}{\varepsilon_0 E} \left\{ \hat{P}_s \tanh \left[\frac{\varepsilon_0 (\varepsilon_g(0) - 1) (E + \hat{E}_c)}{\hat{P}_s} \right] + \hat{P}_s - P_s - \hat{P}_r \right\}$$

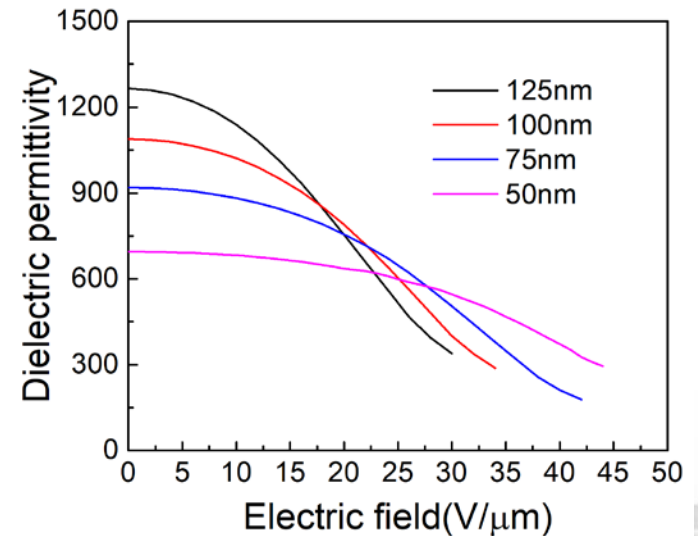
3) Gauss' law

$$\nabla \cdot D = 0.$$

Local electric field distribution

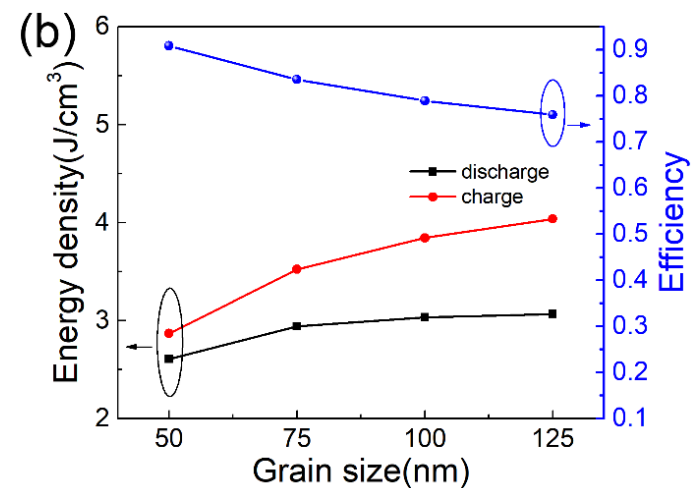
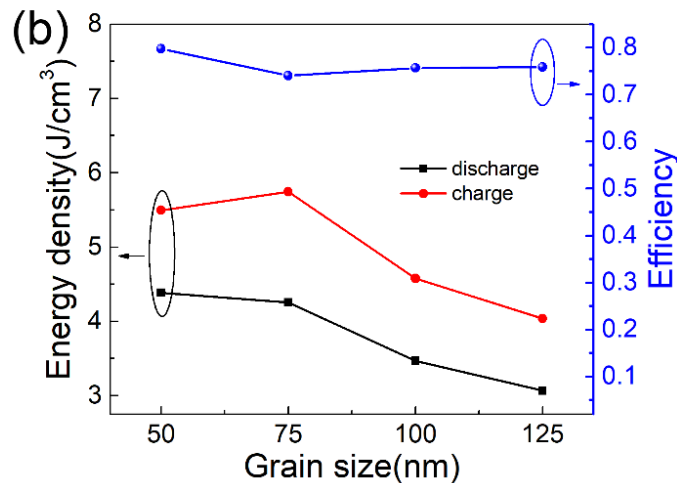
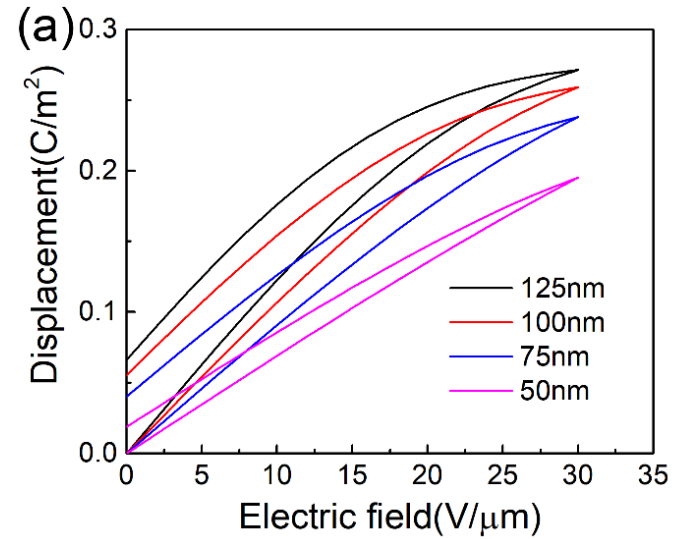
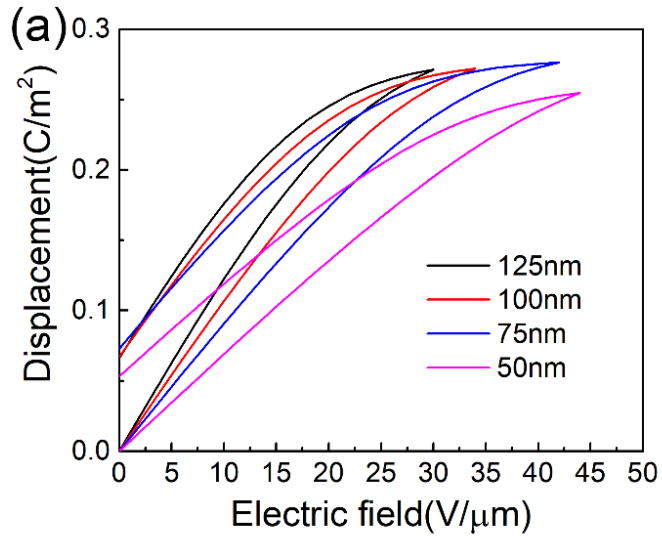


Relative local electric field distribution of these ferroelectric ceramics at various grain size under a given applied electric field of 30 V/μm.



Dielectric permittivity as a function of electric field of the nanostructure ferroelectric ceramics with different grain size.

D-E loop & Energy density



Conclusion



- The ferroelectric hysteresis loop are numerically calculated through a finite element method based on **a classical and modified hyperbolic tangent model**.
- It is found that as the grain size decreases, the dielectric permittivity is reduced. Under the same applied electric field, the ferroelectric ceramic with the smaller grain size possesses a lower discharge energy density but higher energy storage efficiency.
- When the applied electric field reaches their own breakdown strength, the smallest grain-sized ceramic displays the largest discharge energy density and energy storage efficiency.
- It is highly suggested that ferroelectric ceramics with smaller grain sizes can be used for applications in energy storage devices.





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Thanks !

