

Modeling and Simulation of Multicomponent Adsorption of Organic Acids from Aqueous Solutions

Haripriya Naidu

Alexander P. Mathews

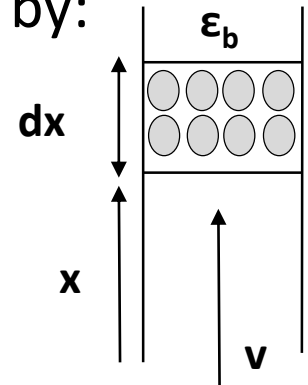
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Governing equations for a fixed-bed adsorber

- Differential mass balance for adsorption of $c(z,t)$ is given by:

Accumulation rate of C = rate of C {[in by dispersion]-[out by dispersion]}
 +[in by convection]-[out by convection]-[loss by adsorption]}



Liquid phase

$$\star 1 \quad -D_L \frac{\partial^2 c}{\partial x^2} + \frac{\partial v c}{\partial x} + \frac{\partial c}{\partial t} + \left(\frac{1 - \epsilon_b}{\epsilon_b} \right) \frac{3}{r_p} k_f (c - c_{p,r=r_p}) = 0$$

Solid phase

$$\star 2 \quad \epsilon_p \frac{\partial c_p}{\partial t} + \rho_p \frac{\partial q_p}{\partial t} = \frac{1}{r^2} \frac{\partial}{\partial r} \left[r^2 \left(\epsilon_p D_p \frac{\partial c_p}{\partial r} \right) \right]$$

$$\star 3 \quad q_p = \frac{q_m k c_p}{1 + k c_p}$$

Initial and boundary conditions

$$0 < x < L, t = 0: c = 0$$

$$x = 0, t > 0: D_L \frac{\partial^2 c}{\partial x^2} = v(c_{x=0} - c_0)$$

$$x = L, t > 0: \frac{\partial c}{\partial x_{x=L}} = 0$$

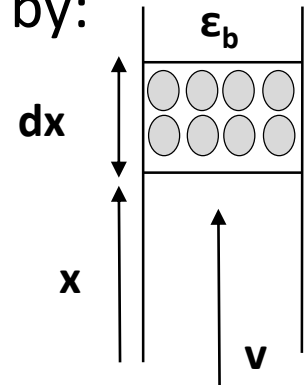
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$$r = 0, t > 0: \frac{\partial c_p}{\partial r}_{r=0} = \frac{\partial q_p}{\partial r}_{r=0} = 0; \quad r = r_p, t > 0: \epsilon_p D_p \frac{\partial c_p}{\partial r}_{r=r_p} = k_f (c - c_{p,r=r_p})$$

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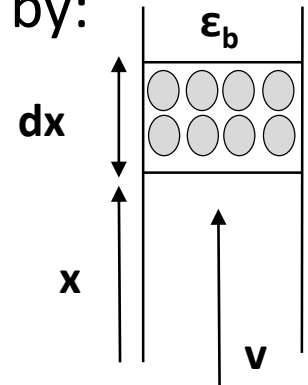
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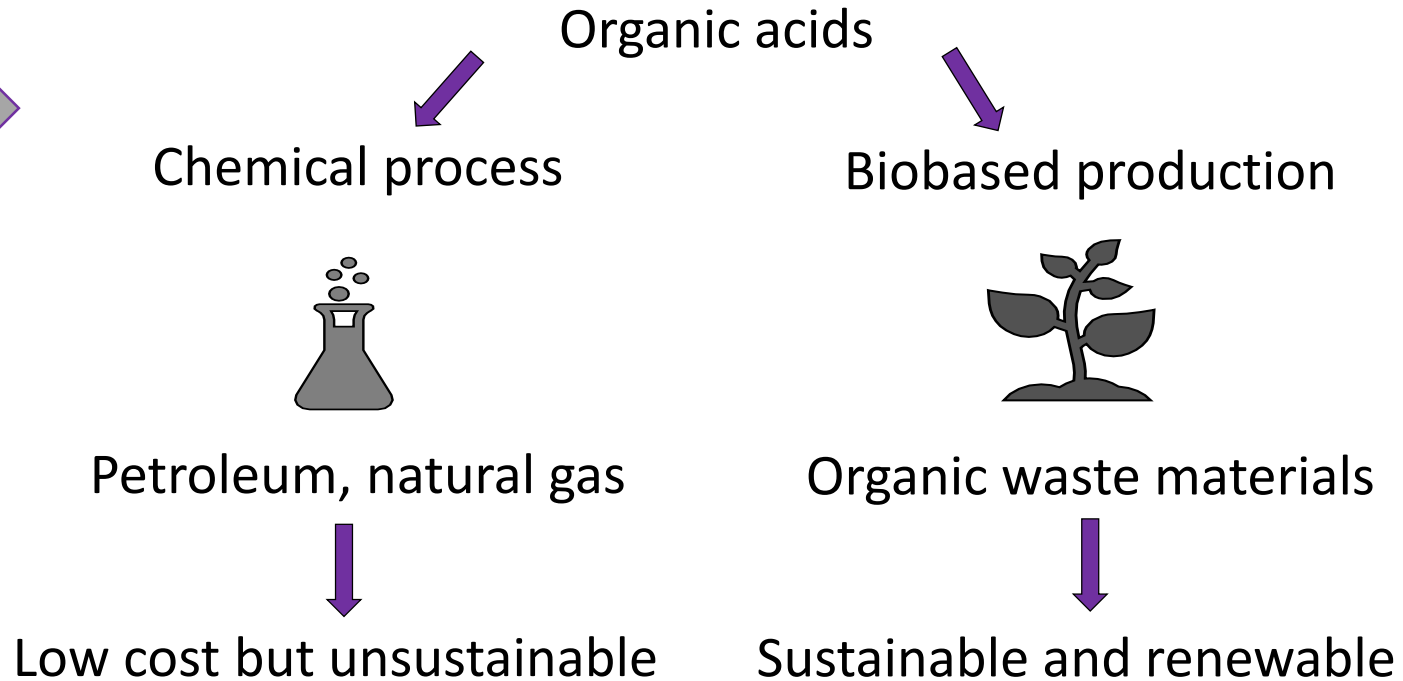
$$r = 0, t > 0: \frac{\partial c_p}{\partial r}_{r=0} = \frac{\partial q_p}{\partial r}_{r=0} = 0; \quad r = r_p, t > 0: \epsilon_p D_p \frac{\partial c_p}{\partial r}_{r=r_p} = k_f (c - c_{p,r=r_p})$$

Outline

- Overview of bioconversion processes to produce organic acids from biomass and biomass wastes
- Downstream separation processes for extraction of organic acids from fermentation broths at low pH
- Adsorption equilibrium and kinetics in the sorption of organic acids
- Fixed-bed sorption dynamics and adsorber configurations for enhanced recovery
- Multicomponent adsorption dynamics

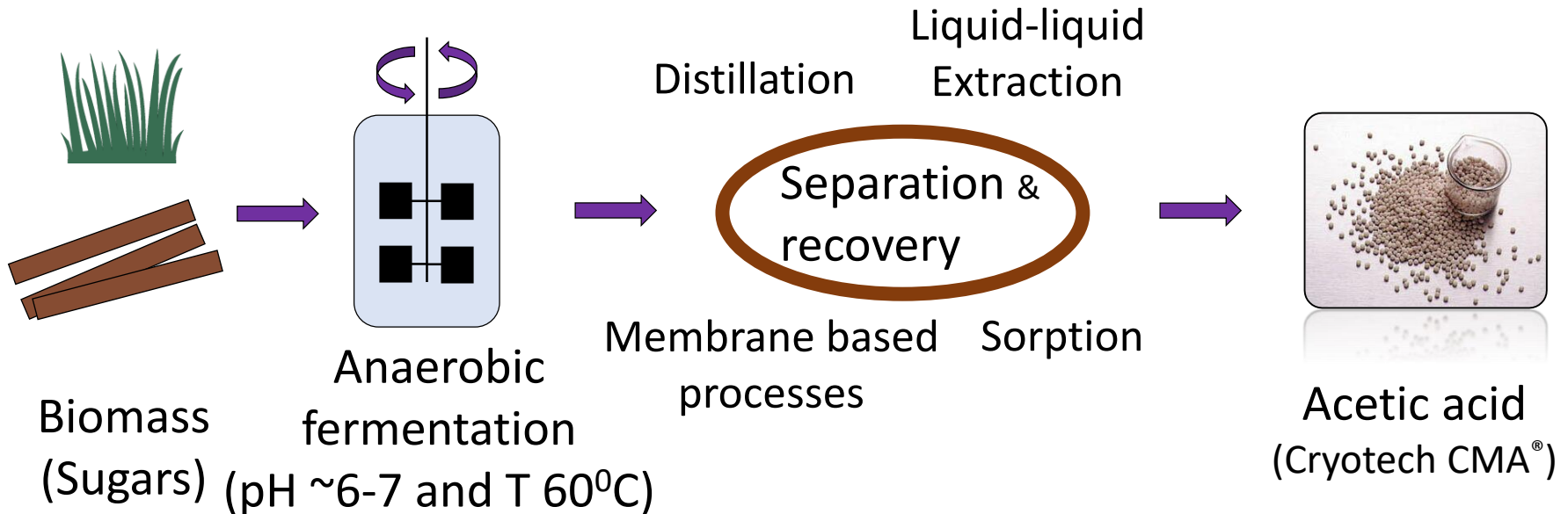
Introduction

Biobased or
chemical
based?



- Global acetic acid demand ~ 13 million tons in 2015¹
- 65% of acetic acid produced via methanol carbonylation²
- Global lactic acid demand expected to reach 1.9 million tons by 2020³
- >90% of lactic acid produced via fermentation³
- By 2100, more than 95% of chemicals and polymers are envisioned to be produced from renewable resources⁴

Production of organic acids from renewable sources and the need for efficient recovery



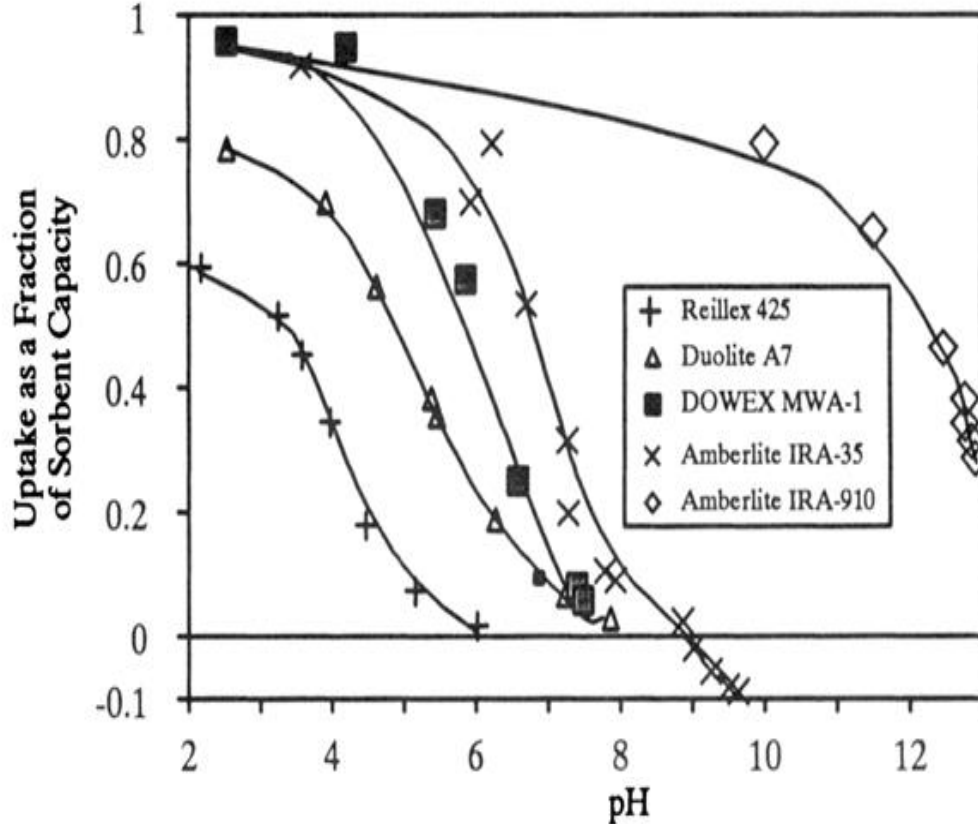
- Acetic acid uses in food, polymer, and other industries. Emerging use in production of calcium magnesium acetate (CMA) road deicer and potassium acetate (KA) aircraft deicer
- CMA from synthetic acetic acid ~\$1900 per ton
- CMA is biodegradable and an environmentally benign alternative for rock salt with a potential demand of 25 million tons per year in North America³

Anaerobic fermentation of carbohydrates to acetic acid

| Bacteria | pH | T |
|--|-----------|----------|
| • <i>Clostridium thermoaceticum</i> | 6.5 – 7.0 | ~ 60°C |
| • <i>C. thermoaceticum</i> and <i>M. thermoautotrophica</i> | 6.4 – 7.0 | ~ 60°C |
| • <i>C. formicoaceticum</i> and <i>L. lactis</i> | 7.6 | ~ 58°C |

Adsorption for recovery of acetic and lactic acids from aqueous solutions

Tung and King, 1994

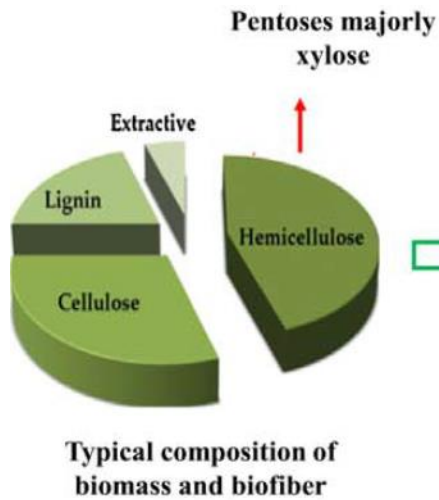


- Uptake capacity of weak base resins decrease with increase in solution pH
- Not feasible to economically recover acetic or lactic acid at neutral pH

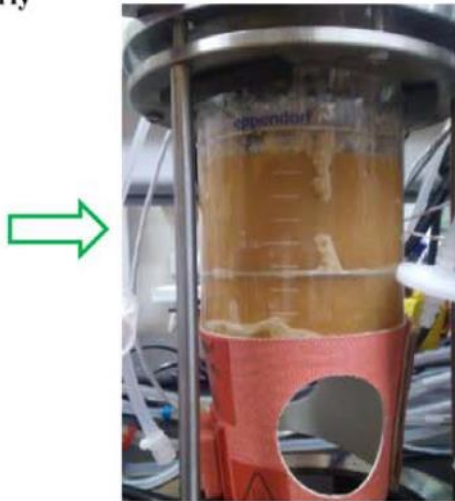
Challenges in the application of bioprocesses for acetic acid production:

- Conduct fermentation at low pH and ambient temperature
- Enhance bed capacity utilization

Novel low pH fermentation process for the production of organic acids from biomass and biomass wastes

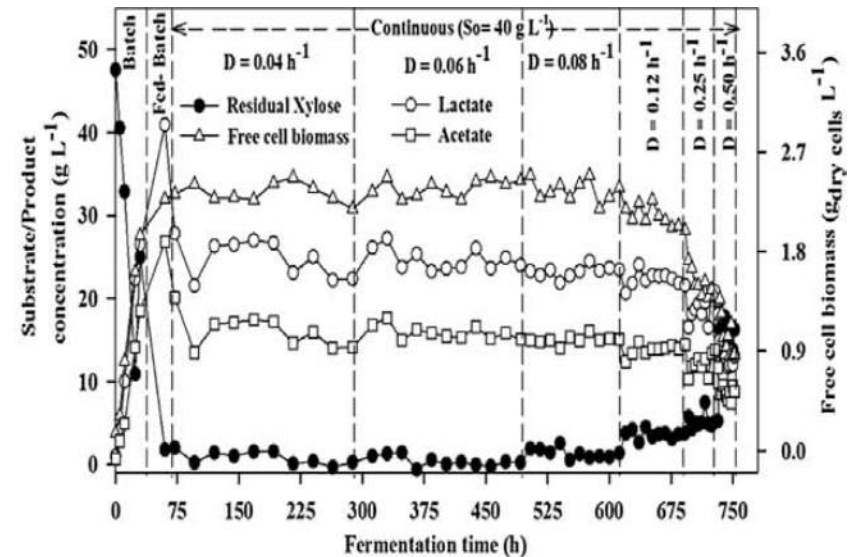


Xylose



L. buchneri immobilized in alumina fibers in CSTR

Anoxic fermentation
(pH ~4 and T 35°C)



Veeravalli and Mathews, 2018

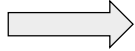
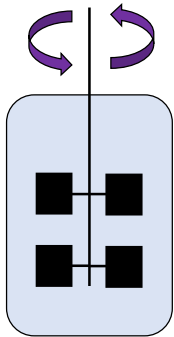
- Novel pH ~4 bacterial fermentation for acetic and lactic acids production using xylose
- 32 g/L acetic acid and 67 g/L lactic acid were produced in fed batch fermentation

Objectives

- Recovery of acetic and lactic acids at low pH using adsorption technology
- Evaluation of adsorption contactor for enhanced bed capacity utilization
- Modeling of sorption process on granular activated carbon (GAC) and synthetic resins
- Implementation of model solution using COMSOL software

Fixed-bed adsorbers to recover organic acids from fermentation broth

Fermentation tank

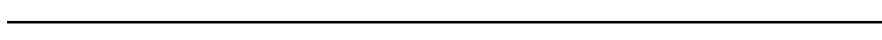


Fixed bed adsorber

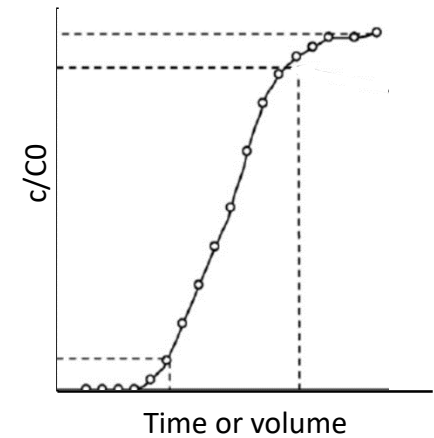
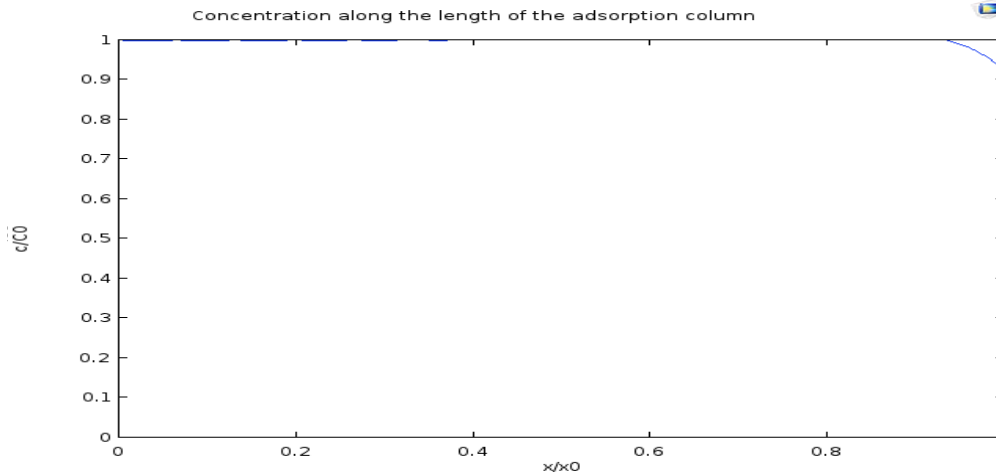


Model

Acetic acid
Lactic acid



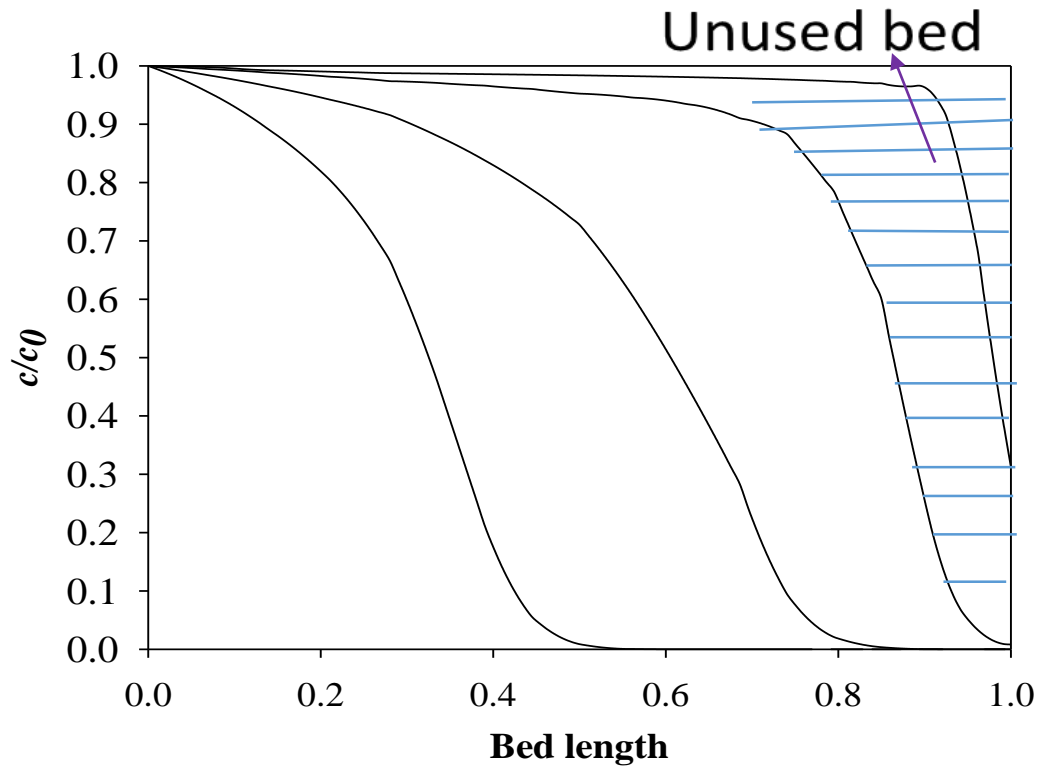
Output



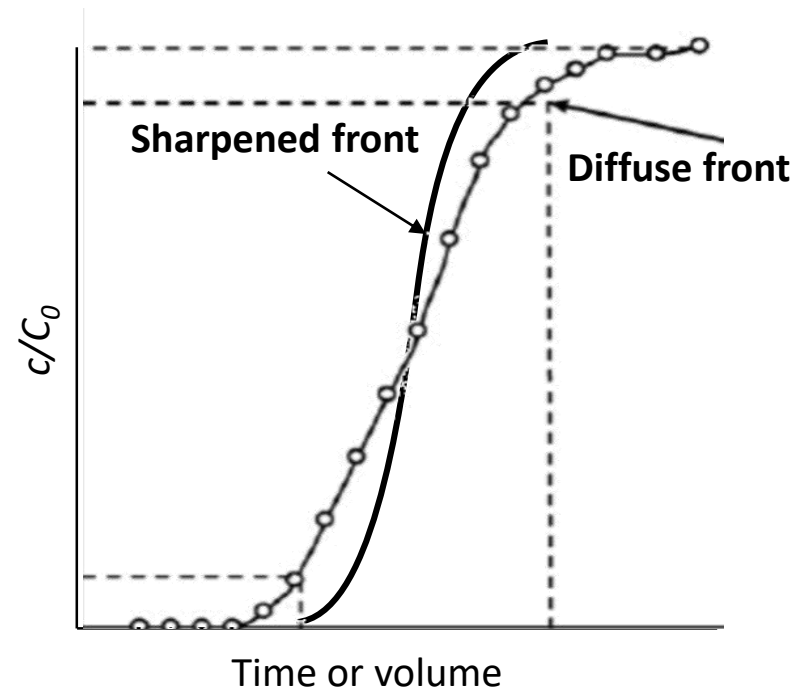
Breakthrough curve

Bed capacity utilization

Concentration profile along the bed length

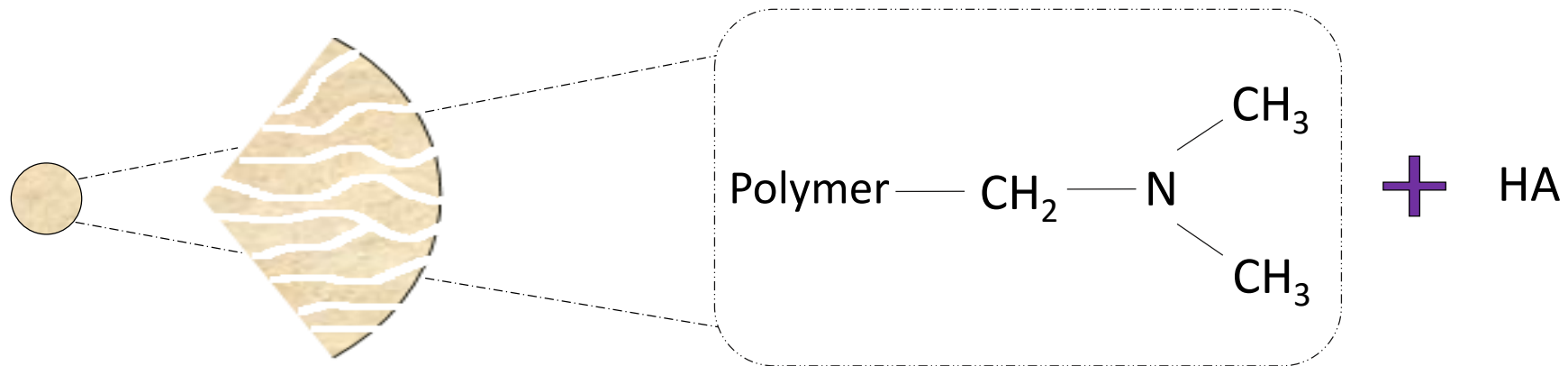


Breakthrough curve

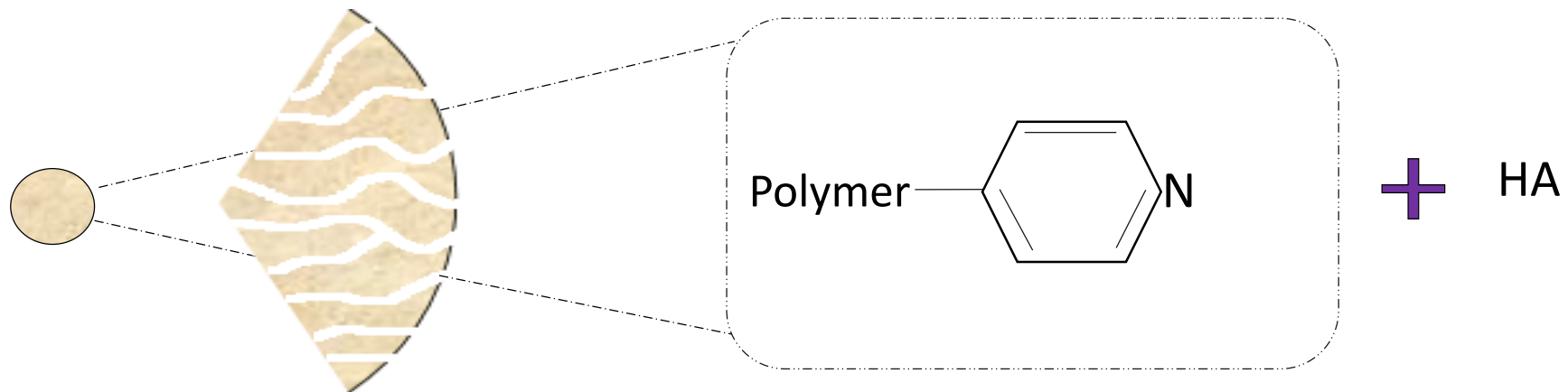


Adsorption of organic acids on weak base resins

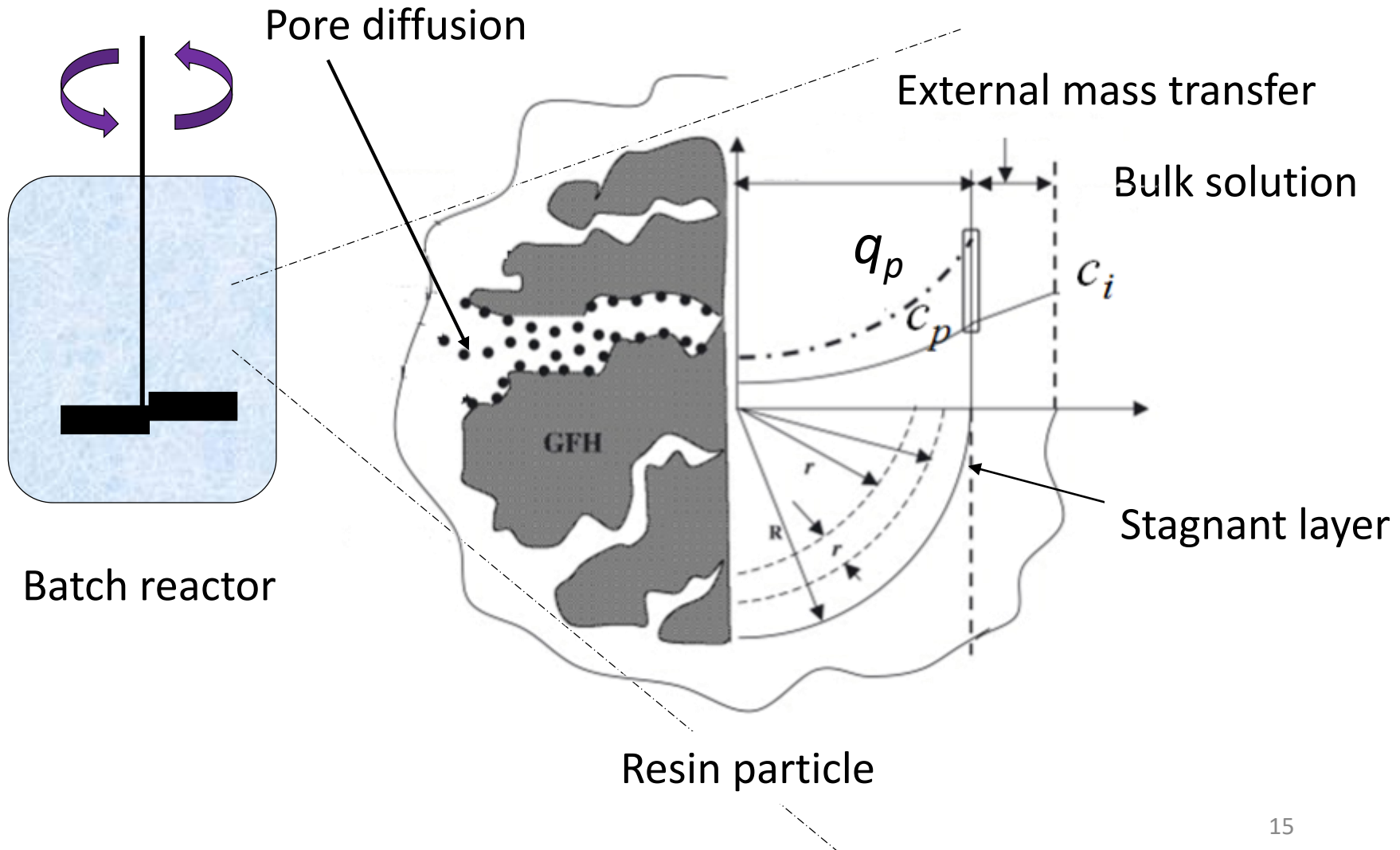
Purolite A835



Reillex 425



Adsorption kinetics: Mass transfer mechanisms in the transport of solute



Governing equations for batch adsorber kinetics

- The differential mass balance for adsorption of $c(z,t)$ is given by:

Bulk phase mass balance

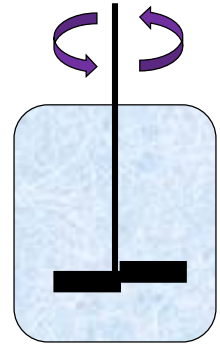
$$V \frac{\partial c_i}{\partial t} + \frac{\partial q_i}{\partial t} = 0$$

Intraparticle transport

$$\frac{\partial q_i}{\partial t} = \frac{1}{r^2} \frac{\partial}{\partial r} \left[r^2 \left(D_i \frac{\partial q_i}{\partial r} \right) \right]$$

Isotherm

$$q_i = \frac{q_{mi} K_i c_i}{1 + \sum_j^k K_j c_j}$$



Batch reactor

Initial and boundary conditions

$$t = 0: c_i = c_{0i}$$

$$0 < r < r_p, t = 0: q_i = 0$$

$$r = 0, t > 0: \frac{\partial q_i}{\partial r} \Big|_{r=0} = 0;$$

$$r = r_p, t > 0: D_i \frac{\partial q_i}{\partial r} \Big|_{r=r_p} = k_f (c_i - c_{pi,r=r_p})$$

Governing equations for batch adsorber kinetics

- The differential mass balance for adsorption of $c(z,t)$ is given by:

Particle phase mass balance

$$\frac{\partial q}{\partial t} = D_c \left(\frac{\partial^2 q}{\partial r^2} + \frac{2}{r} \frac{\partial q}{\partial r} \right)$$

Initial and boundary conditions

$$q(r, 0) = q'_0 \quad \frac{\partial q}{\partial r} = 0$$

$$q(rc, 0) = q_0 \quad \frac{\partial q}{\partial r} = 0$$

Analytical solution

$$\alpha < 0.1$$

$$1 - \frac{m_t}{m_\infty} \approx \frac{6}{\pi^2} \exp\left(-\frac{\pi^2 D_c t}{r_c^2}\right)$$

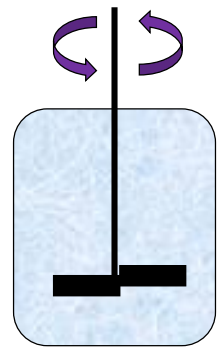
$$\alpha = \frac{C_0 - C_\infty}{C_0}$$

Analytical solution

$$\alpha > 0.1$$

$$\frac{m_t}{m_\infty} = 1 - 6 \sum_{n=1}^{\infty} \frac{\exp\left(-\frac{p_n^2 D_c t}{r_c^2}\right)}{\frac{9\alpha}{(1-\alpha)} + (1-\alpha)p_n^2}$$

$$\tan p_n = \frac{3p_n}{3 + \left(\frac{1}{\alpha} - 1\right)p_n^2}$$

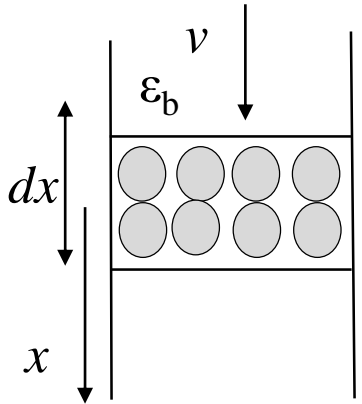


Batch reactor

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Bulk phase mass balance

$$-D_{Li} \frac{\partial^2 c_i}{\partial x^2} + v \frac{\partial c_i}{\partial x} + \frac{\partial c_i}{\partial t} + \left(\frac{1 - \varepsilon_b}{\varepsilon_b} \right) \frac{3}{r_p} k_{fi} (c_i - c_{pi, r=r_p}) = 0$$

Intraparticle transport

$$\varepsilon_p \frac{\partial c_{pi}}{\partial t} + \rho_p \frac{\partial q_{pi}}{\partial t} = \frac{1}{r^2} \frac{\partial}{\partial r} \left[r^2 \left(\varepsilon_p D_{pi} \frac{\partial c_{pi}}{\partial r} \right) \right]$$

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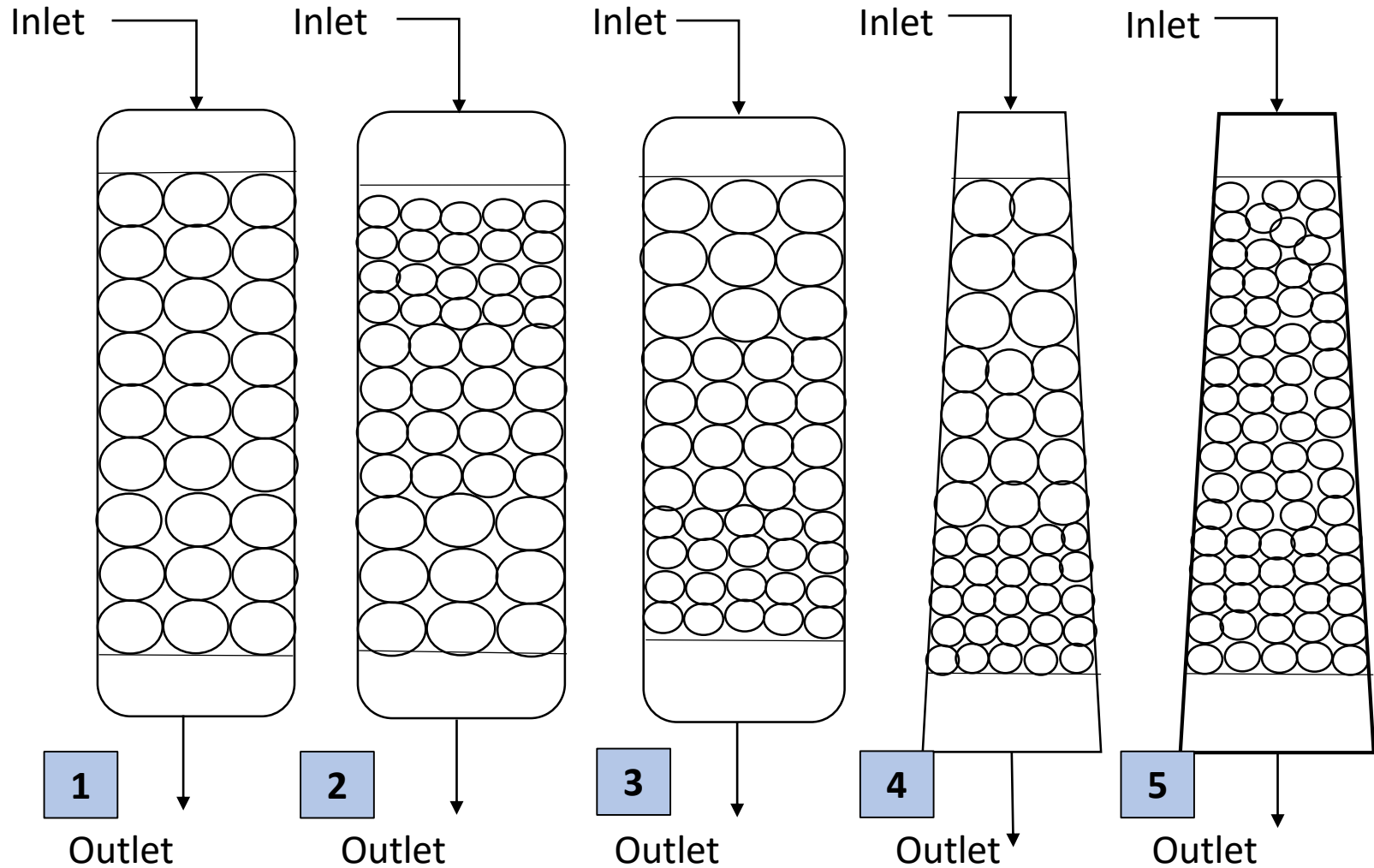
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$$r = r_p, t > 0: \varepsilon_p D_{pi} \frac{\partial c_{pi}}{\partial r} \Big|_{r=r_p} = k_{fi} (c_i - c_{pi, r=r_p})$$

Materials and Methods: Fixed-bed adsorber configurations



Adsorber configurations: (1) conventional cylindrical adsorber (CCA) with single particle size, (2) normally stratified cylindrical adsorber (SCA), (3) reverse stratified cylindrical adsorber, (4) reverse stratified tapered adsorber (RSTA), and (5) tapered bed with single particle size 19

Physicochemical properties of granular activated carbon and operational parameters

| Property | | Stratified adsorber | |
|--|-------|---------------------------------|--------------------|
| Particle size (cm) | 0.065 | Mesh fraction | Particle size (cm) |
| Bulk density (g/cm ³) | 0.701 | 18-20 | 0.092 |
| Particle porosity | 0.66 | 20-25 | 0.077 |
| | | 25-30 | 0.065 |
| | | 30-35 | 0.055 |
| Operational parameters | | 35-40 | 0.046 |
| Amount of resin (g) | 40 | | |
| Superficial velocity (cm/min) | 2.36 | | |
| Bed length (cm) | 20 | Tapered bed adsorber dimensions | |
| Bed diameter (cm) | 2.54 | Bed length (cm) | 14.4 |
| Inlet concentration of Acetic acid (g/L) | 15 | Bed diameter top (cm) | 2 |
| | | Bed diameter bottom (cm) | 4 |
| Isotherm constant, a (g/g) | 0.186 | | |
| Isotherm constant, b (L/g) | 0.53 | | |

Physicochemical properties of Purolite A835 resin and operational parameters

| Property | | Stratified adsorber | |
|--|-------|---------------------------------|--------------------|
| Particle size (cm) | 0.065 | Mesh fraction | Particle size (cm) |
| Wet particle density (g/cm ³) | 1.072 | 20-25 | 0.077 |
| Particle porosity | 0.28 | 25-30 | 0.065 |
| | | 30-35 | 0.055 |
| | | Operational parameters | |
| Amount of resin (g) | 62 | Tapered bed adsorber dimensions | |
| Superficial velocity (cm/min) | 2.36 | Bed length (cm) | 13.25 |
| Bed length (cm) | 18 | Bed diameter top (cm) | 2.44 |
| Bed diameter (cm) | 2.54 | Bed diameter bottom (cm) | 3.5 |
| Inlet concentration of Acetic acid (g/L) | 15 | pH of Multicomponent studies | |
| Maximum adsorption capacity, q_{max} (g/g) | 0.27 | 2.8 | 4.8 |
| Isotherm constant, k (L/g) | 0.506 | | |

Operational parameters

Axial dispersion coefficient

(Suzuki and Smith, 1972)

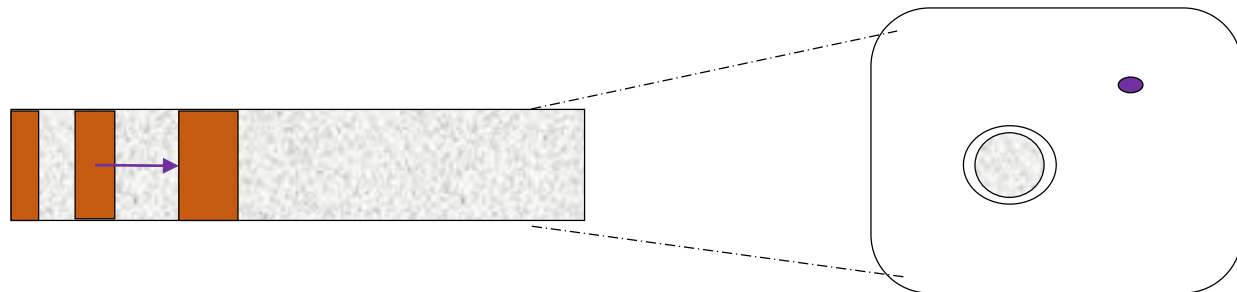
External mass transfer coefficient

(Dwivedi and Upadhyay, 1977)

Pore diffusion coefficient

(Mackie and Maeres, 1955)

| Component | D_L (cm ² /min) | K_f (cm/min) | D_p (*10 ⁴ cm ² /min) |
|-------------|------------------------------|----------------|---|
| Acetic acid | 0.128 | 0.101 | 2.7 |
| Component | D_L (cm ² /min) | K_f (cm/min) | D_p (*10 ⁵ cm ² /min) |
| Acetic acid | 0.128 | 0.018 | 6.6 |
| Lactic acid | 0.095 | 0.016 | 2.7 |



Implementation in COMSOL Multiphysics®

• MI

The image displays the COMSOL Multiphysics software interface, showing the Model Builder tree on the left and a plot window on the right. The Model Builder tree is organized into two components, Component 1 (comp1) and Component 2 (comp2). Both components have a similar structure of definitions, geometry, materials, and meshing. The plot window on the right shows a convergence plot for a study named 'Study 1'.

Model Builder Tree Structure:

- Hac_GAC_GRM_3-26-18.mph (root)
 - Global Definitions
 - Parameters
 - Materials
 - Component 1 (comp1)
 - Definitions
 - Variables 1
 - General Extrusion 1 (genext1)
 - View 1
 - Geometry 1
 - Interval 1 (i1)
 - Form Union (fin)
 - Materials
 - Coefficient Form PDE (c)
 - Coefficient Form PDE 1
 - Zero Flux 1
 - Initial Values 1
 - Flux/Source 1
 - Equation View
 - Mesh 1
 - Component 2 (comp2)
 - Definitions
 - Geometry 2
 - Rectangle 1 (r1)
 - Form Union (fin)
 - Materials
 - Coefficient Form PDE 2 (c2)
 - Coefficient Form PDE 1
 - Zero Flux 1
 - Initial Values 1
 - Flux/Source 1
 - Equation View
 - Mesh 2
 - Study 1
 - Step 1: Time Dependent
 - Solver Configurations
 - Results
 - Data Sets
 - Derived Values
 - Tables
 - Table 1
 - 1D Plot Group 1
 - Point Graph 1

Implementation in COMSOL Multiphysics®

Coefficient form PDE interface in COMSOL Multiphysics®

Model Builder

Settings
Coefficient Form PDE

Label: Coefficient Form PDE 1

Domain Selection

Show equation assuming:
Study 1, Time Dependent

$$e_a \frac{\partial^2 C_a}{\partial t^2} + d_a \frac{\partial C_a}{\partial t} + \nabla \cdot (-c \nabla C_a - \alpha C_a + \gamma) + \beta \cdot \nabla C_a + a C_a = f$$

$$\nabla = \frac{\partial}{\partial x}$$

Domain

$$n \cdot (c \nabla u + \alpha u - \gamma) + q u = g - h^T \mu$$

$$u = r$$

Domain boundary

Diffusion Coefficient
c: Diax_a

Absorption Coefficient
a: 0

Source Term
f: $-(1-\text{epsb})/\text{epsb} * (3/\text{rp}) * \text{kf}_a * (C_a - C_{\text{pel}_a})$

Mass Coefficient
e_a: 0

Damping or Mass Coefficient
d_a: 1

Messages
Progress
Log
Table 1

Solution time (Study 1): 16 s.
Number of degrees of freedom solved for: 2678 (plus 1770 internal DOFs).
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Solution time (Study 1): 16 s.
Number of degrees of freedom solved for: 2678 (plus 1770 internal DOFs).
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Number of degrees of freedom solved for: 2678 (plus 1770 internal DOFs).
Solution time (Study 1): 15 s.
Saved file: H:\Breakthrough curves_PBAST\Hac_GAC_GRM_3-26-18.mph

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Application Builder Component Parameters a= Variables f(x) Functions Build All Import Add Material Coefficient Form PDE Add Physics Build Mesh Mesh 1 Compute Study Add Study 1D Plot Group 5 Add Plot Group Windows Reset Desktop

Model Builder

SCA_GRM_DCP_330.mph (root)

- Global Definitions
 - Parameters
 - Materials
- Phenol (comp1)
 - Definitions
 - Geometry 1
 - Interval 1 (i1)
 - Point 4 (pt4)
 - Point 5 (pt5)
 - Point 6 (pt6)
 - Point 7 (pt7)
 - Point 8 (pt8)
 - Point 9 (pt9)
 - Point 10 (pt10)
 - Point 1 (pt1)
 - Point 2 (pt2)
 - Point 3 (pt3)
 - Point 11 (pt11)
 - Form Union (fin)
 - Materials
 - Coefficient Form PDE (c)
 - Coefficient Form PDE 1
 - Zero Flux 1
 - Initial Values 1
 - Flux/Source 2
 - Coefficient Form PDE 2
 - Coefficient Form PDE 3
 - Coefficient Form PDE 4
 - Coefficient Form PDE 5
 - Coefficient Form PDE 6
 - Coefficient Form PDE 7
 - Coefficient Form PDE 8
 - Mesh 1
 - Component 2 (comp2)
 - Definitions
 - Geometry 2
 - Rectangle 1 (r1)
 - Rectangle 2 (r2)
 - Rectangle 3 (r3)
 - Rectangle 4 (r4)
 - Rectangle 5 (r5)
 - Rectangle 6 (r6)
 - Rectangle 7 (r7)

Settings

Coefficient Form PDE

Label: Coefficient Form PDE 1

Domain Selection

Selection: All domains

| ON | 1 |
|----|----------------|
| | 2 (overridden) |
| | 3 (overridden) |
| | 4 (overridden) |
| | 5 (overridden) |
| | 6 (overridden) |

Override and Contribution

Equation

Diffusion Coefficient

c DL1

Absorption Coefficient

a 0

Source Term

f $-((1-\text{epsb})/\text{epsb})*(3/\text{rp1})*\text{kmap1}*(\text{C}_a-\text{Cpe1}_a)$

Mass Coefficient

e_a 0

Damping or Mass Coefficient

d_a 1

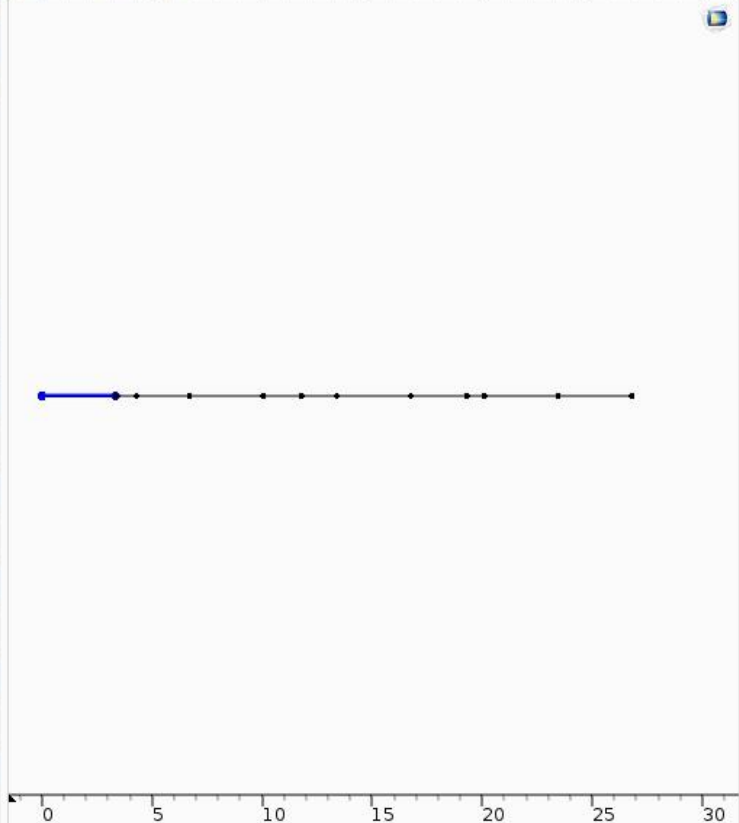
Conservative Flux Convection Coefficient

Convection Coefficient

Conservative Flux Source

Graphics

Graphics toolbar with icons for zoom, pan, and other view controls.



Messages Progress Log Table 2

COMSOL Multiphysics 5.3.0.316
 Opened file: E:\Phenol_DCP\DCP_Phenol_GRM\SCA_GRM_DCP_330.mph

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Application Builder Component Parameters Variables Functions Build All Add Material Coefficient Form PDE 2 Add Physics Build Mesh Mesh 2 Compute Study Add Study 1D Plot Group 5 Add Plot Group Windows Reset Desktop

Model Builder

SCA_GRM_DCP_330.mph (root)

- Global Definitions
 - Parameters
- Materials
 - Phenol (comp1)
 - Definitions
 - Geometry 1
 - Materials
 - Coefficient Form PDE (c)
 - Mesh 1
- Component 2 (comp2)
 - Definitions
 - Geometry 2
 - Rectangle 1 (r1)
 - Rectangle 2 (r2)
 - Rectangle 3 (r3)
 - Rectangle 4 (r4)
 - Rectangle 5 (r5)
 - Rectangle 6 (r6)
 - Rectangle 7 (r7)
 - Rectangle 8 (r8)
 - Form Union (fin)
 - Materials
 - Coefficient Form PDE 2 (c2)
 - Coefficient Form PDE 1
 - Zero Flux 1
 - Initial Values 1
 - Coefficient Form PDE 2
 - Coefficient Form PDE 3
 - Coefficient Form PDE 4
 - Coefficient Form PDE 5
 - Coefficient Form PDE 6
 - Coefficient Form PDE 7
 - Coefficient Form PDE 8
 - Flux/Source 1
 - Flux/Source 2
 - Flux/Source 3
 - Flux/Source 4
 - Flux/Source 5
 - Flux/Source 6
 - Flux/Source 7
 - Flux/Source 8
 - Mesh 2

- Study

Settings

Geometry

Build All

Label: Geometry 2

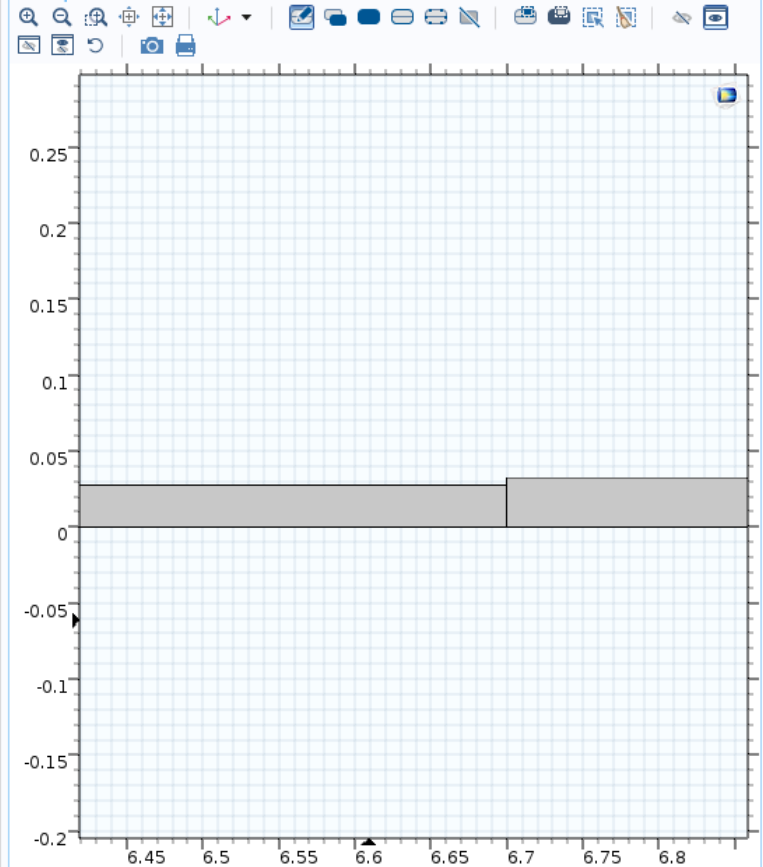
Advanced

Default repair tolerance:

Automatic

Automatic rebuild

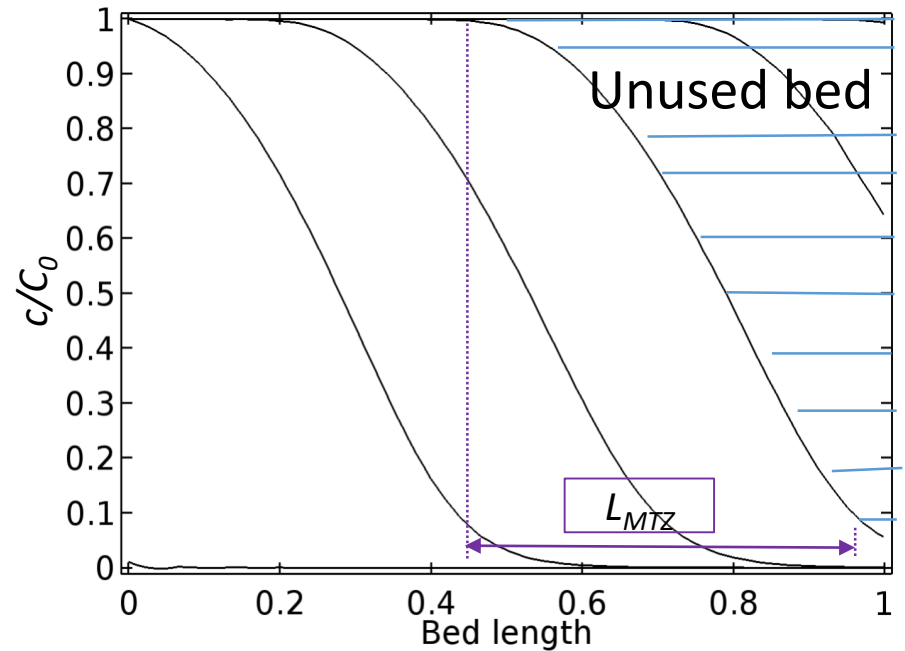
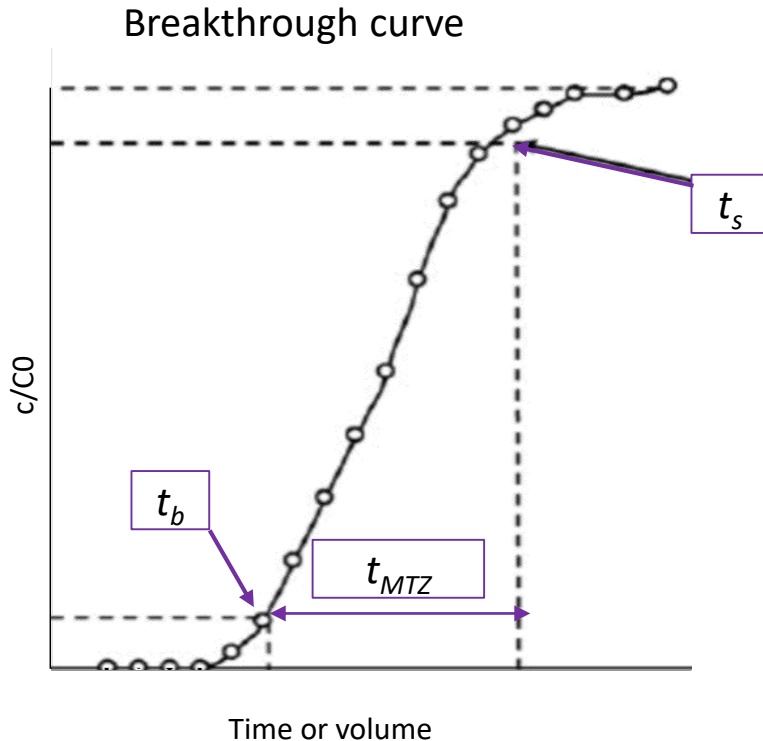
Graphics



Messages Progress Log Table 2

COMSOL Multiphysics 5.3.0.316
 Opened file: C:\Comsol Data Files\Phenol_DCP\DCP_Pheno_GRM\SCA_GRM_DCP_330.mph

Bed capacity utilization

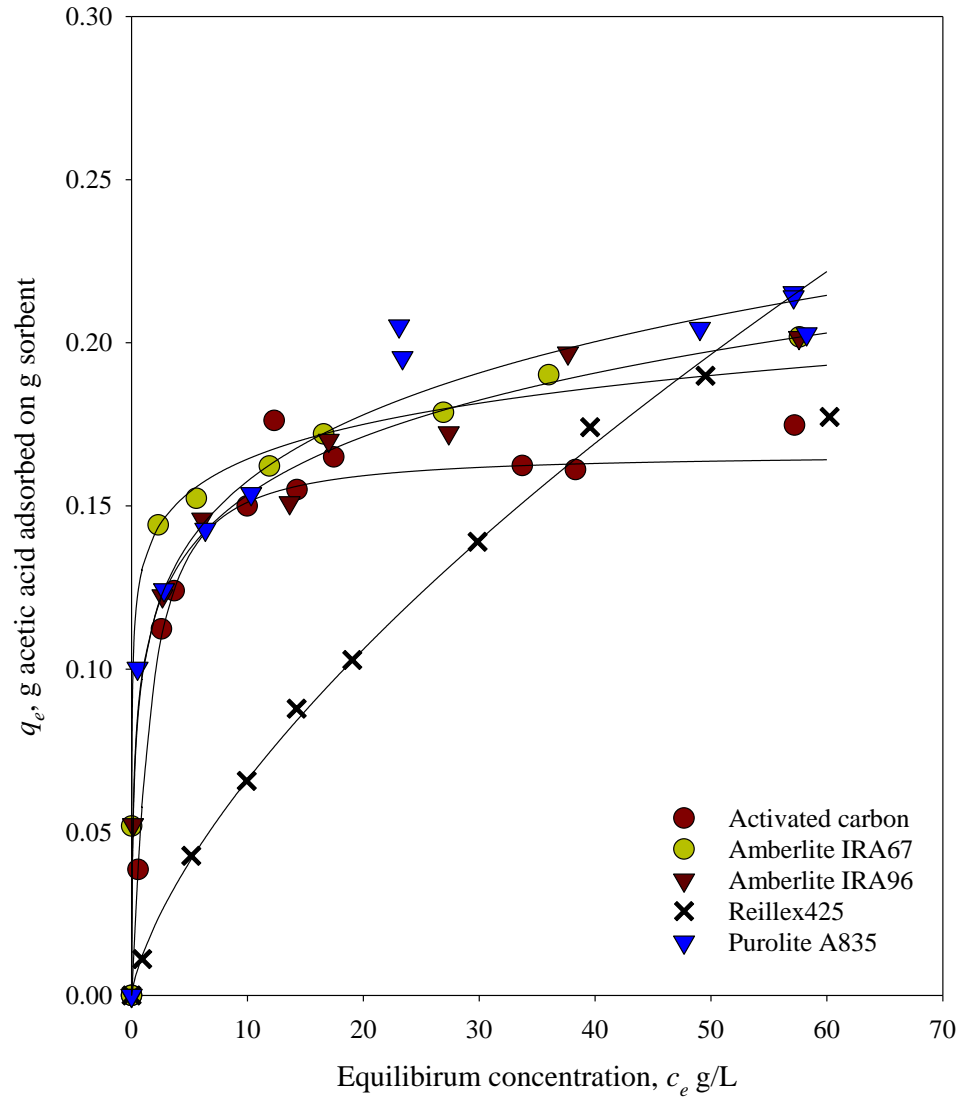


$$L_{MTZ} = U_{sh} t_{MTZ}$$

$$U_{sh} = \frac{V}{\left(1 + \frac{(1 - \varepsilon_b)}{\varepsilon_b} \rho_p \frac{q_0}{C_0}\right)}$$

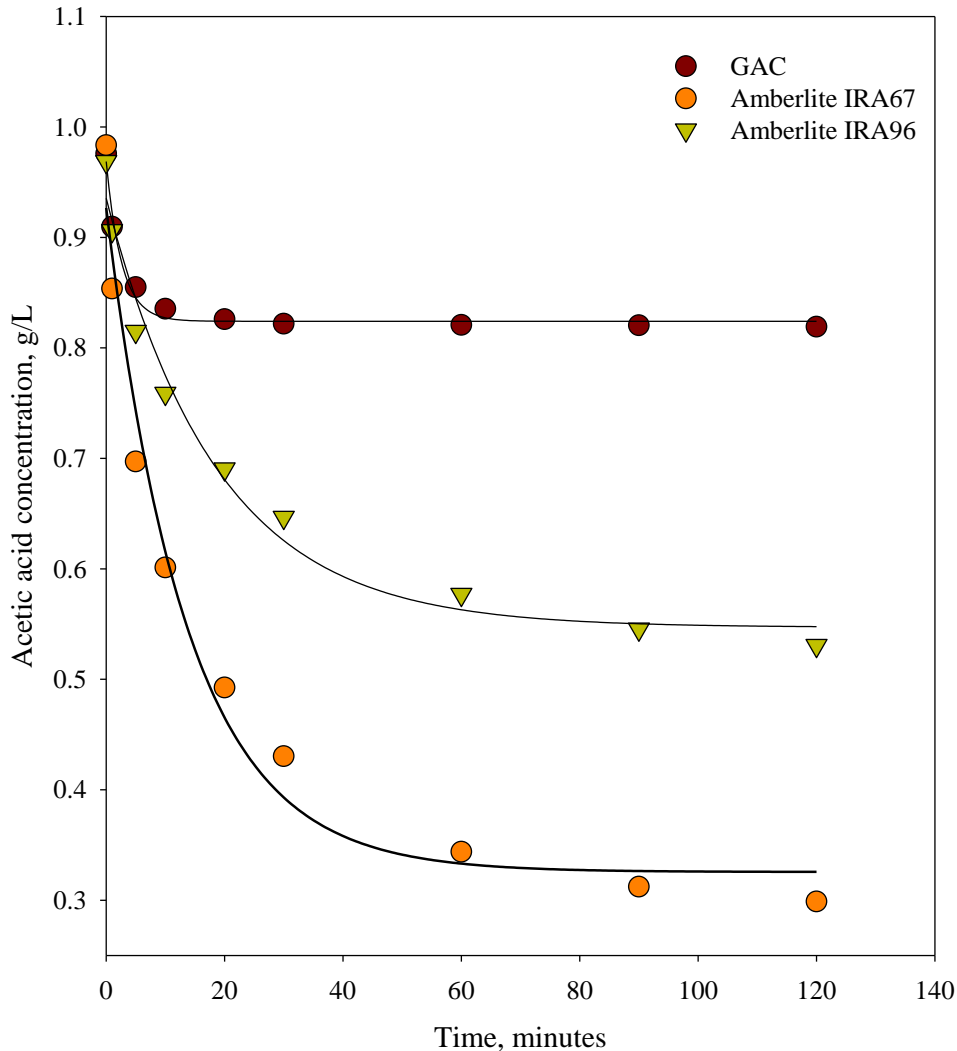
$$\text{fractional bed capacity utilization} = 1 - 0.5 * \frac{L_{MTZ}}{L}$$

Single component adsorption equilibria of acetic acid: Experimental data



- Uptake capacities of weak base resins were higher compared to GAC
- Purolite A835 had highest sorption capacity among the sorbents

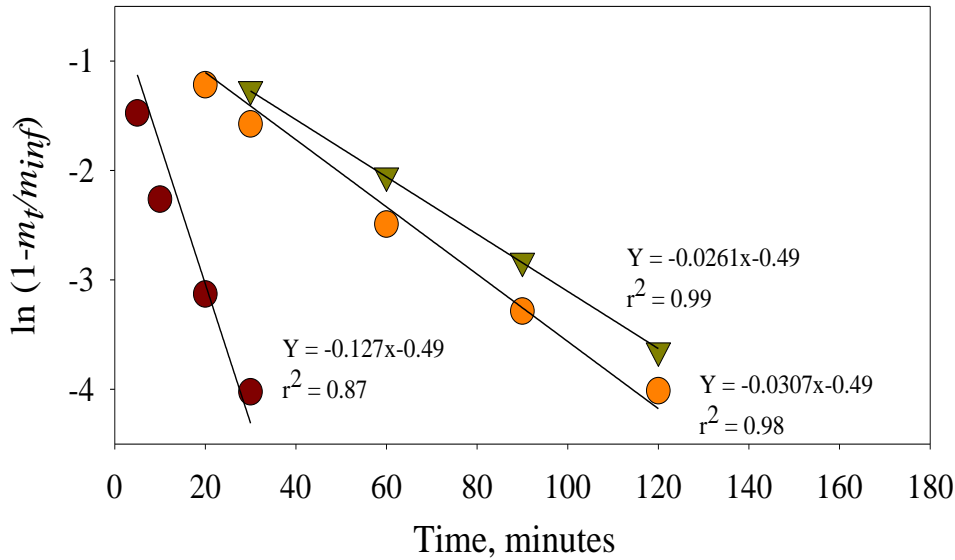
Adsorption kinetics of acetic acid on GAC and resins: Experimental data



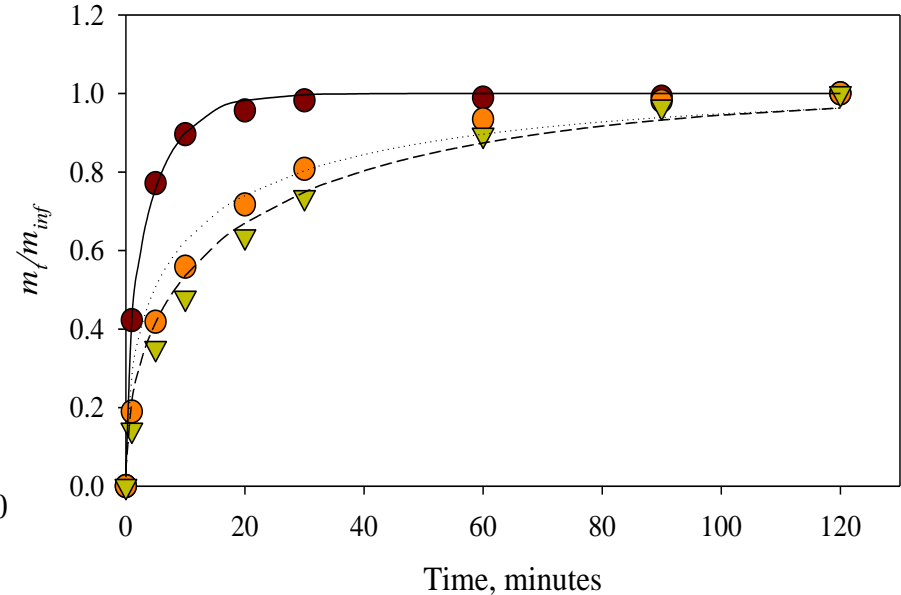
- All sorbents show a common pattern of rapid decrease in first few minutes
- It is followed by little or no change in concentration over the time range studied

Adsorption kinetics of acetic acid on GAC and resins: Kinetic parameters

Linearized equation of infinite bath system



Nonlinear finite bath equation



● Activated carbon ● Amberlite IRA67 ▼ Amberlite IRA96

- External mass transfer coefficient, k_f , is determined using: $k_f = \frac{\rho_p r_p}{3W} \frac{\ln\left(\frac{C_0}{C}\right)}{t}$
- Intraparticle diffusivity, D_c , is obtained using linearized equation obtained for infinite bath system and nonlinear finite bath system equation

Adsorption kinetics of acetic acid on GAC and resins: Kinetic parameters

| | GAC | Amberlite IRA67 | Amberlite IRA96 |
|---|---------|-----------------|-----------------|
| k_f (cm/sec) | 1.98E-3 | 5.33E-3 | 2.72E-3 |
| D_c (cm ² /sec) Equation (4.7) | 1.59E-7 | 0.530E-7 | 0.537E-7 |
| D_c (cm ² /sec) Equation (4.9) | 1.94E-7 | 0.158E-7 | 0.304E-7 |
| ARE | 1.17 | 11.23 | 11.08 |

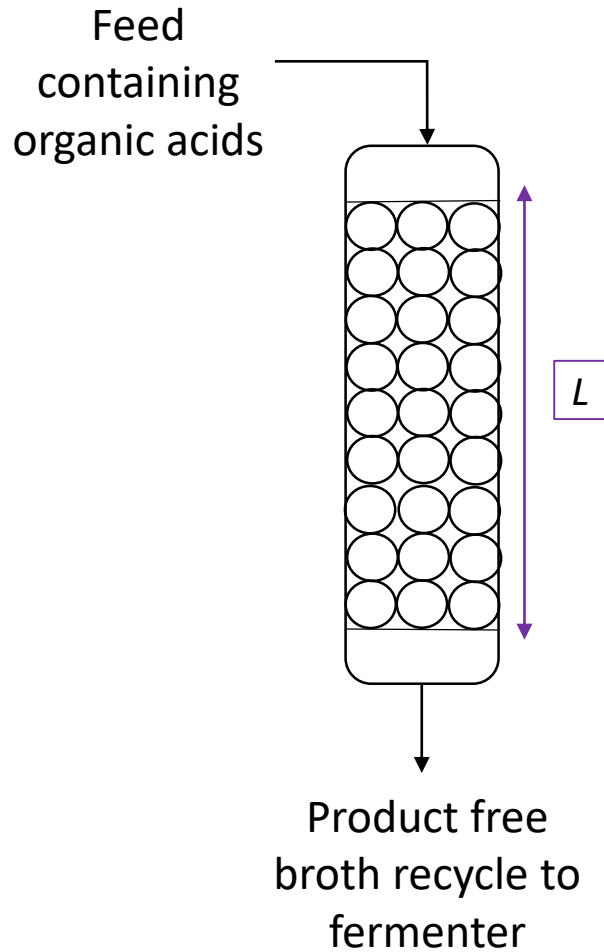
- k_f was lower for GAC because of its low sorption capacity and the low sorbent to solute ratio (0.375 g/L) used to effectively suspend it
- k_f of Amberlite IRA67 was higher than that of the Amberlite IRA96
- For GAC, α was 0.15, and D_c obtained from the finite system equation is 22% higher than that from the infinite volume system equation.
- But, D_c obtained for Amberlite IRA67 and Amberlite IRA96 resins are much more different from each other as α values were 0.69 and 0.45, respectively.

Single component adsorption dynamics in stratified beds

Single component adsorption dynamics

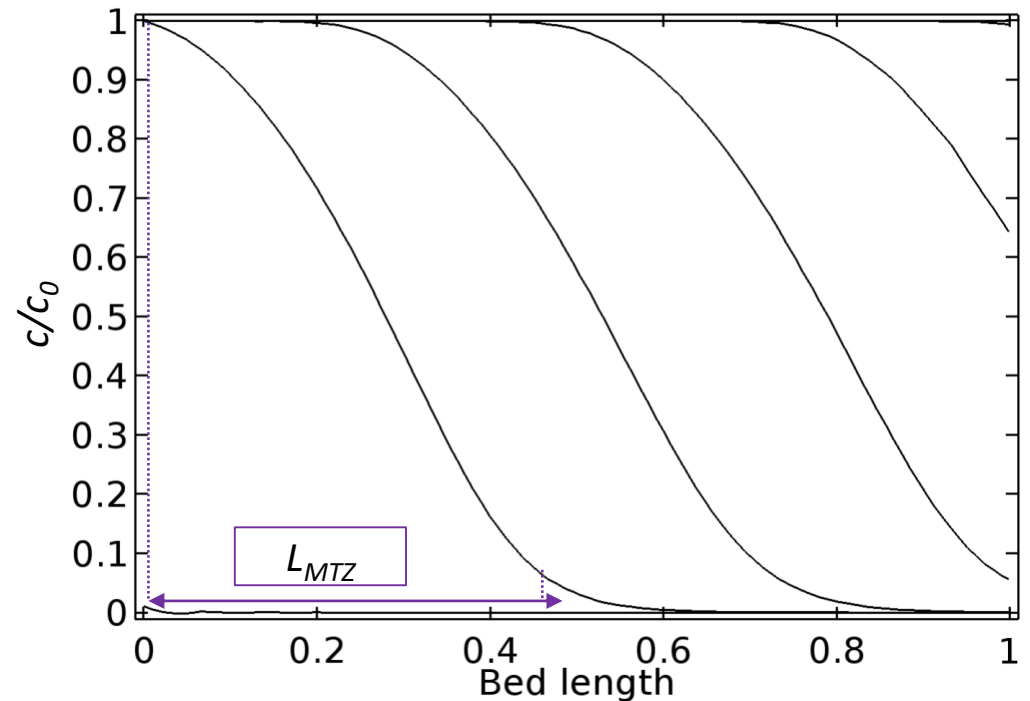
Cylindrical column

Single adsorbent particle size



Concentration profile along the bed length

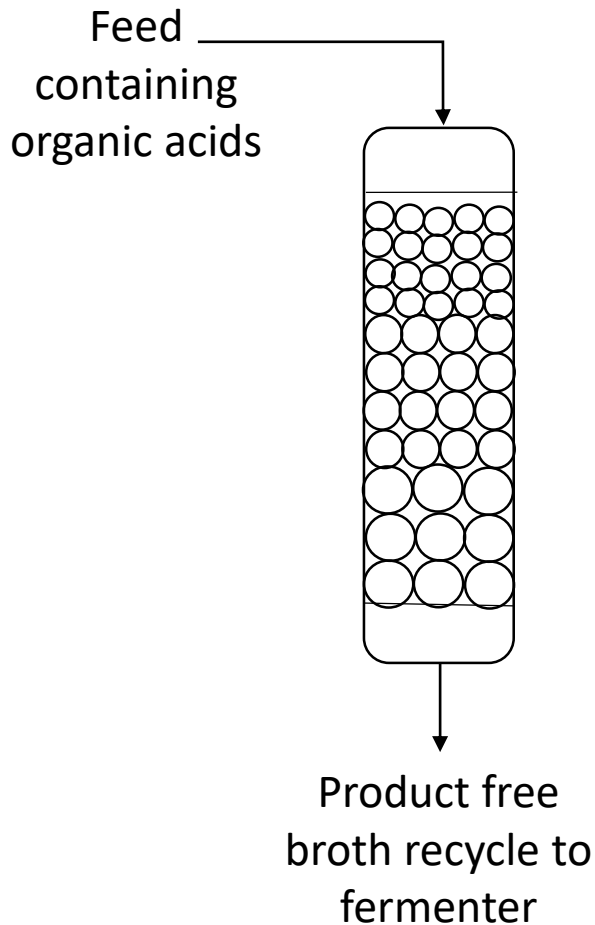
Constant pattern solute front



Single component adsorption dynamics

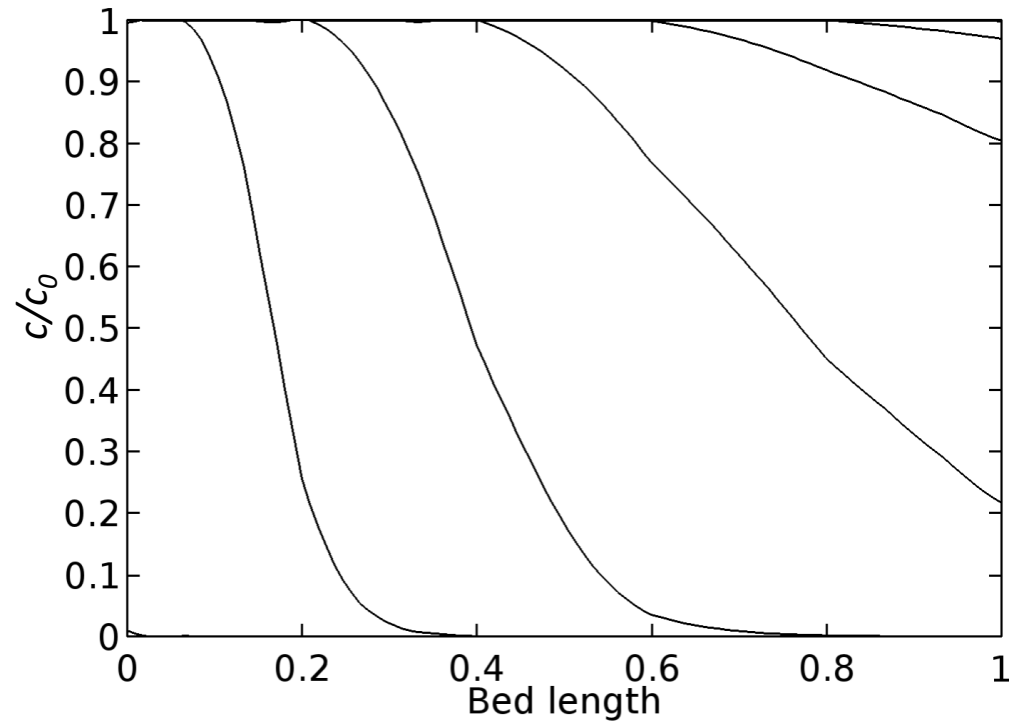
Cylindrical column

Normal stratification



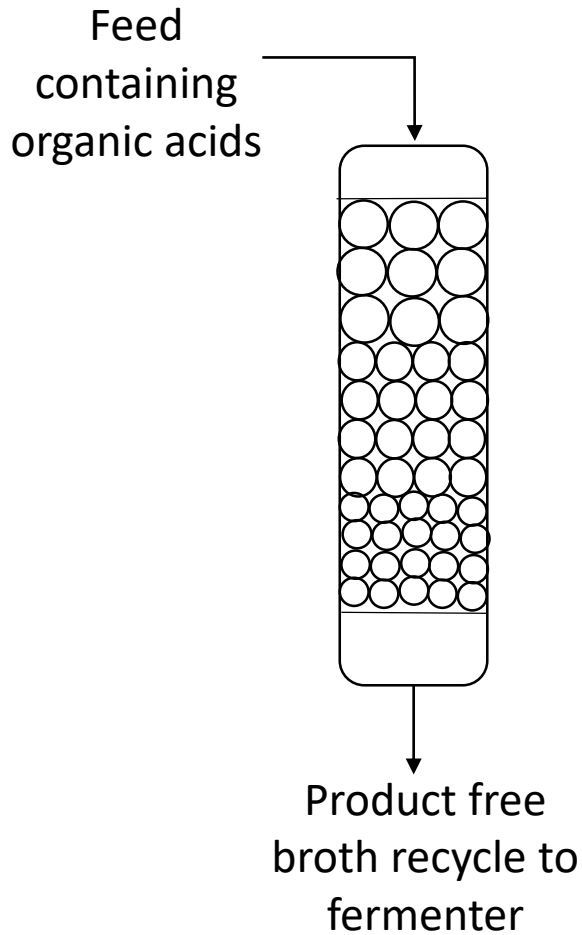
Concentration profile along the bed length

Dispersive solute front



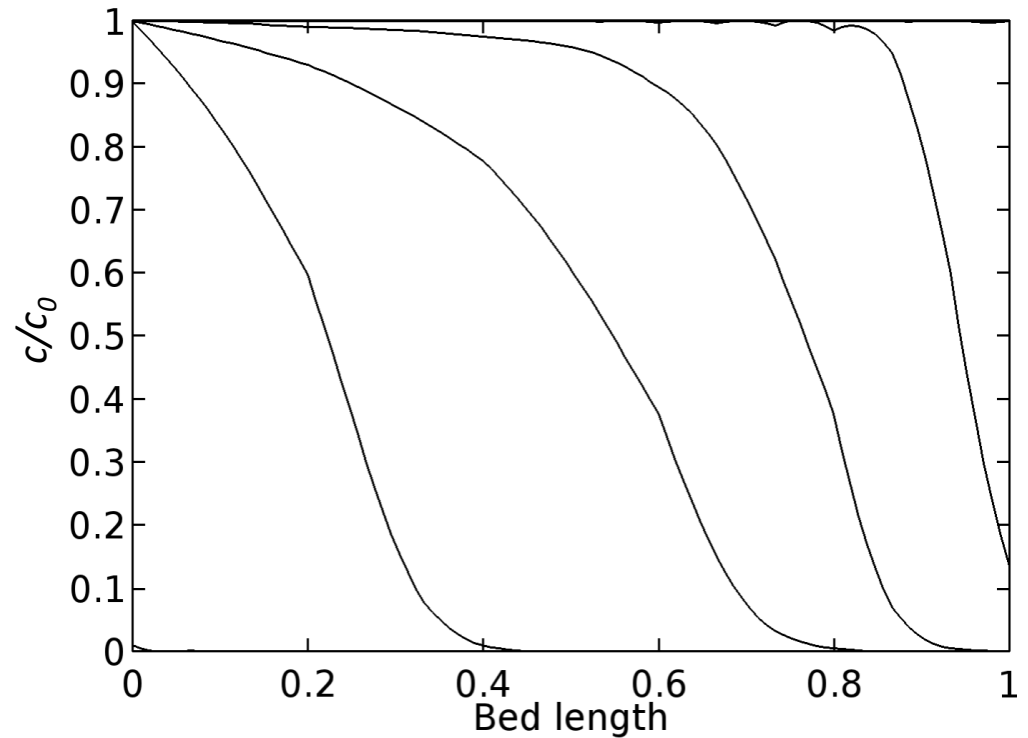
Single component adsorption dynamics

Cylindrical column
Reverse stratification



Concentration profile along the bed length

Sharpening solute front

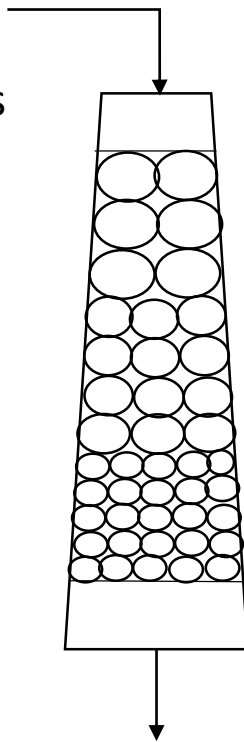


Single component adsorption dynamics

Tapered column

Reverse stratification

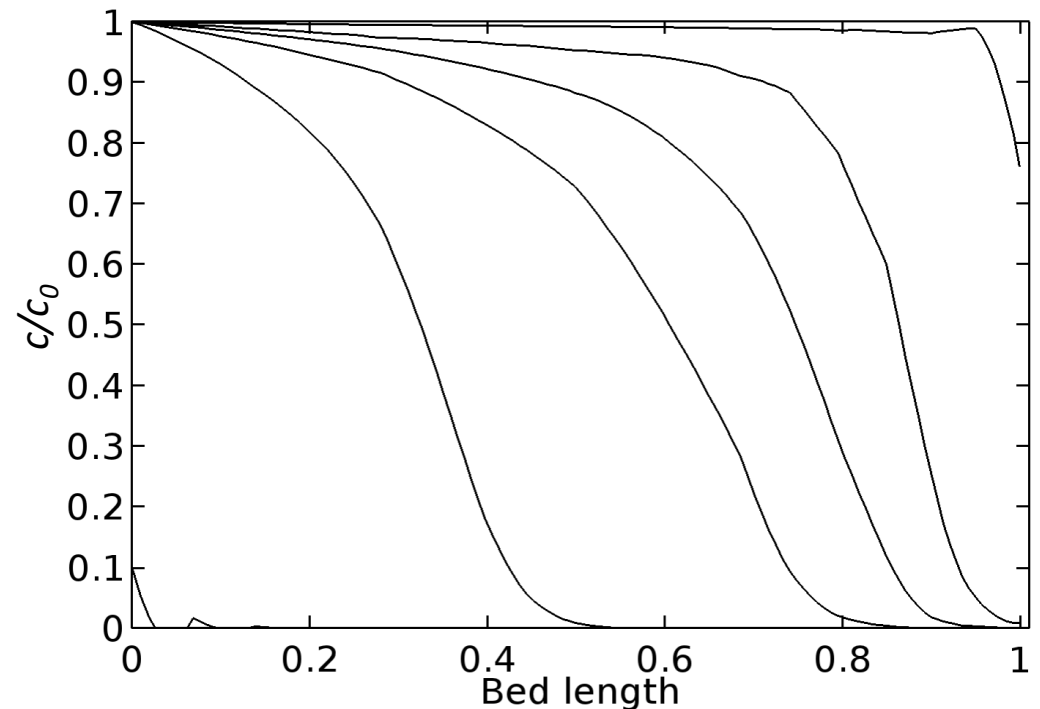
Feed
containing
organic acids



Product free
broth recycle to
fermenter

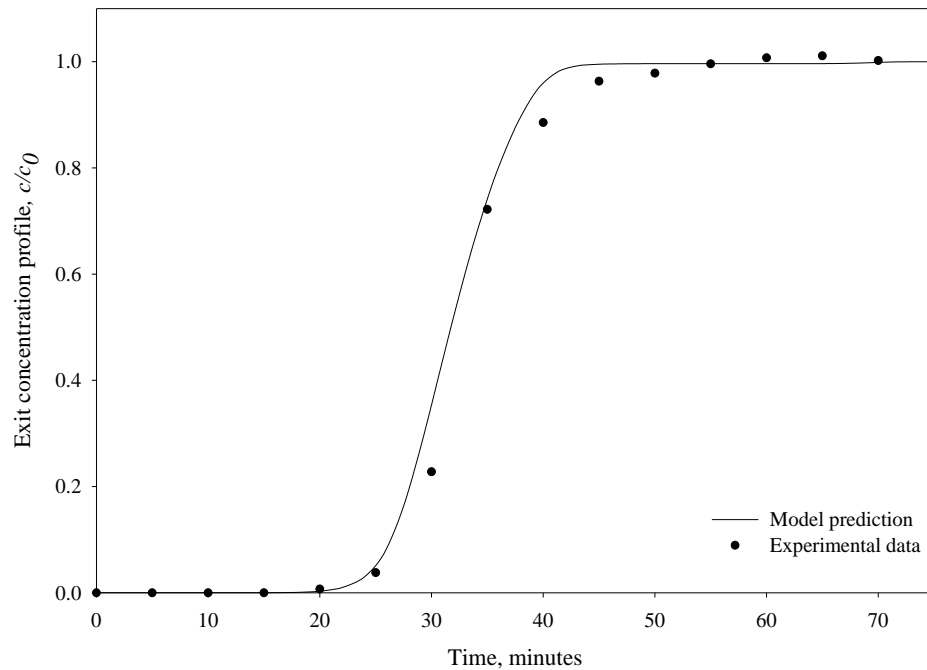
Concentration profile along the bed length

Sharpening solute front

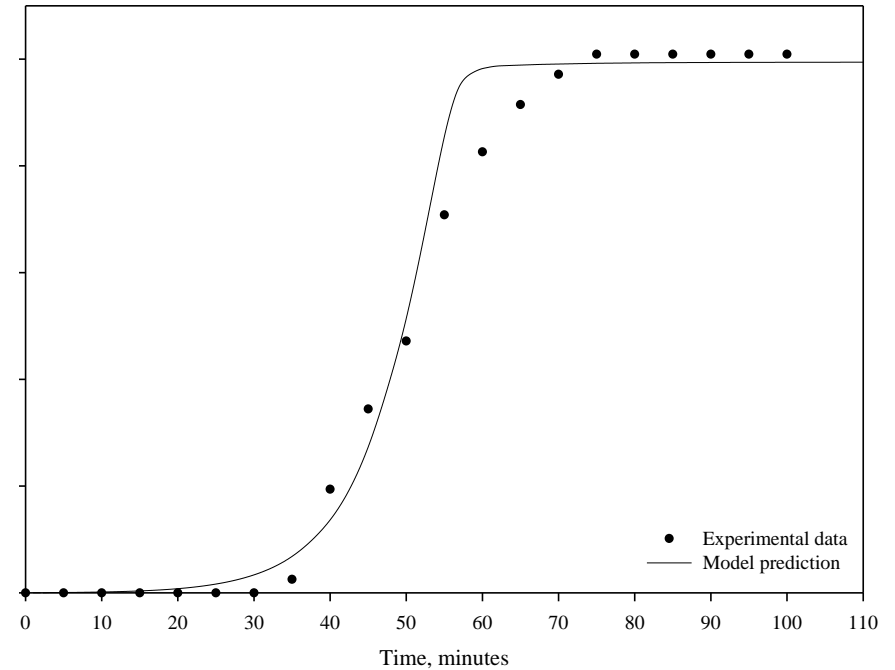


Breakthrough curve analysis

Cylindrical adsorber with single adsorbent particle size



GAC

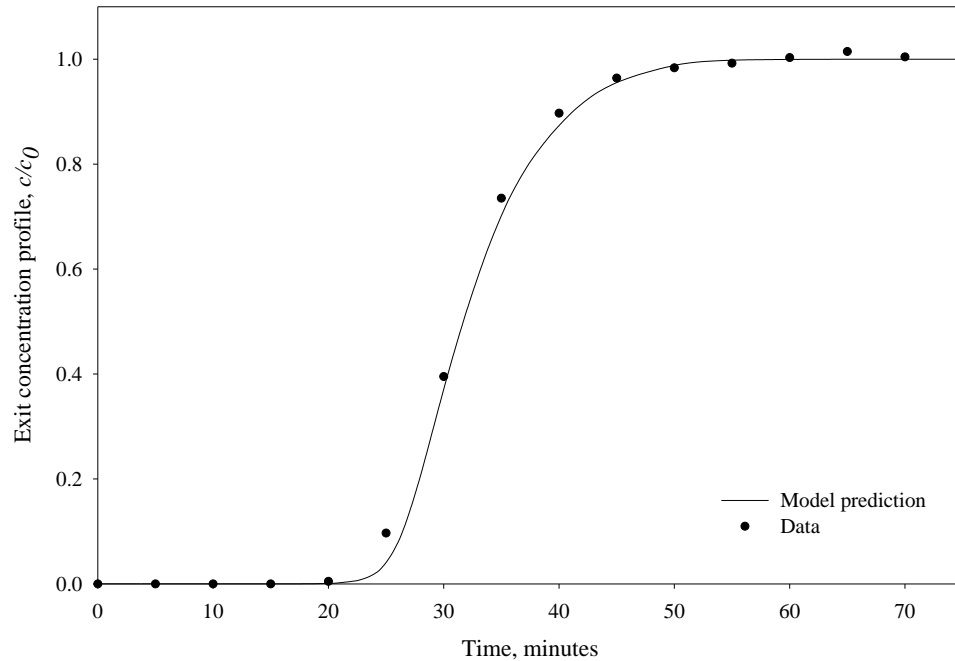


Purolite A835

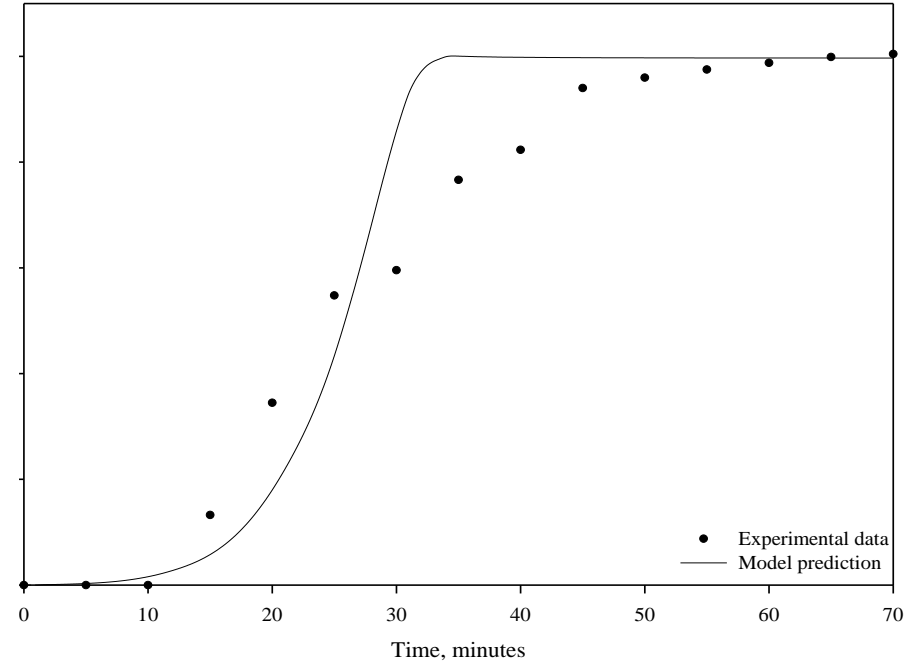
- Constant pattern solute front develops
- Mass transfer effects are uniform along bed length

Breakthrough curve analysis

Cylindrical adsorber with normally stratified adsorbent



GAC

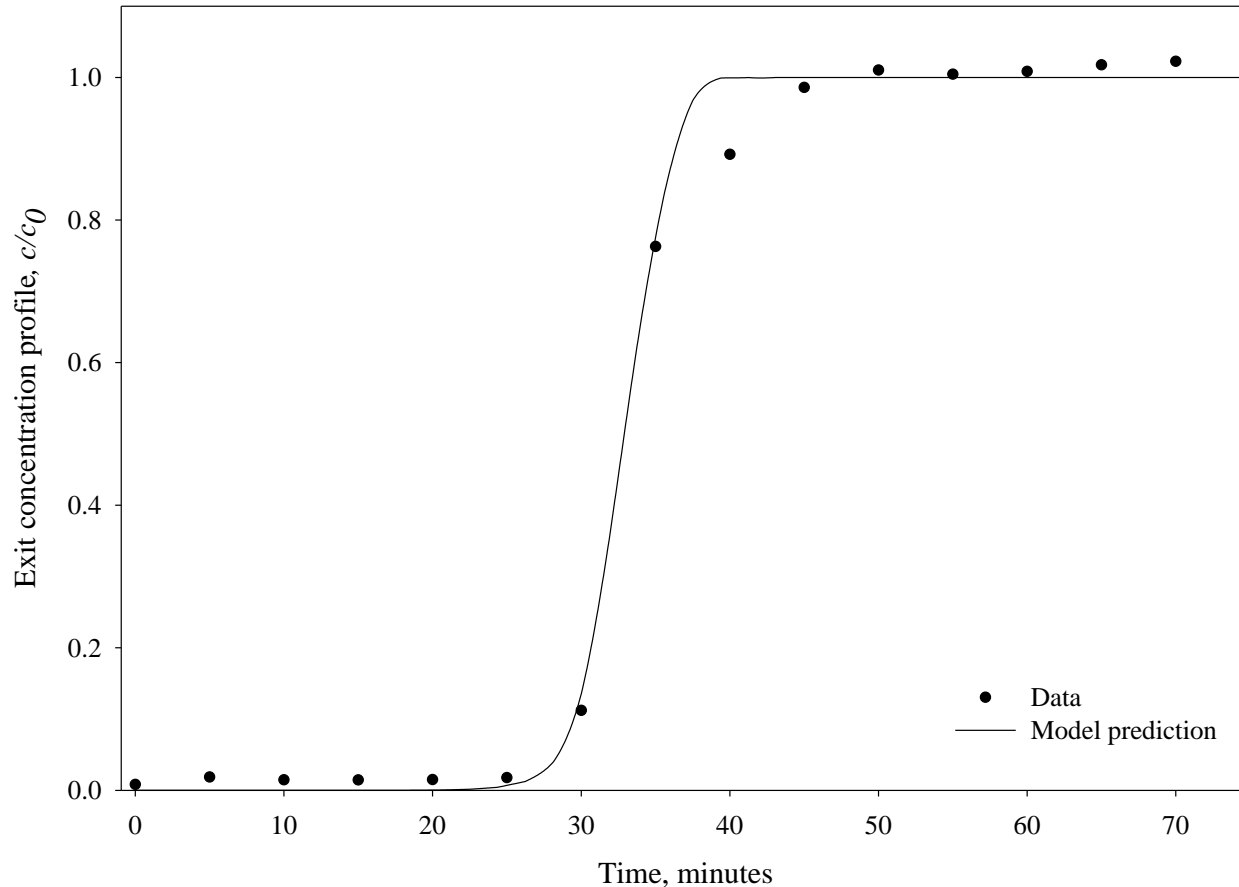


Purolite A835

- Solute front disperses along the bed length
- t_b decreases and t_s increases

Breakthrough curve analysis

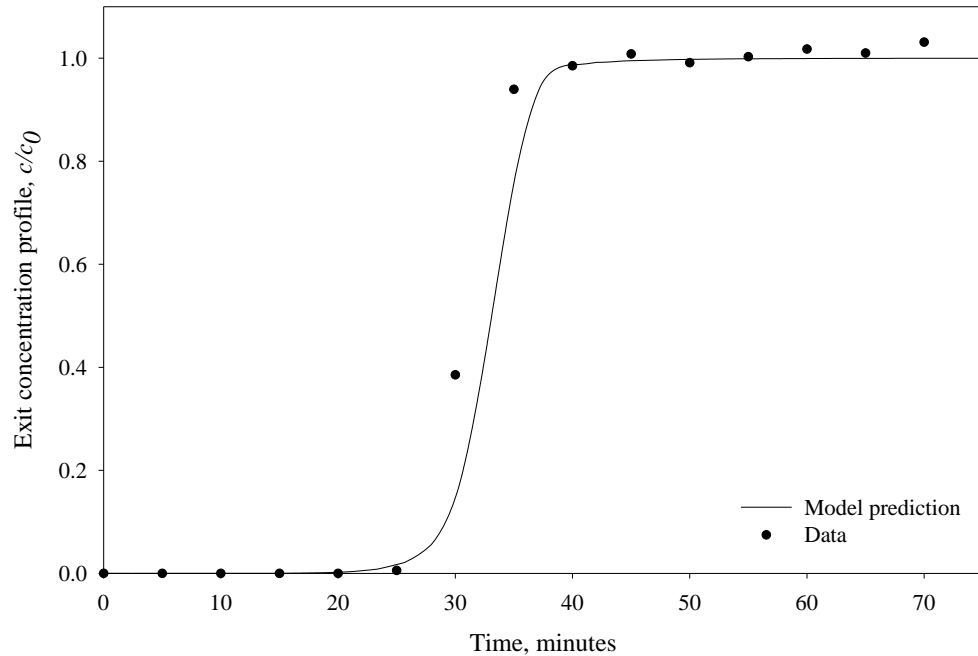
Cylindrical adsorber with reverse stratified adsorbent (GAC)



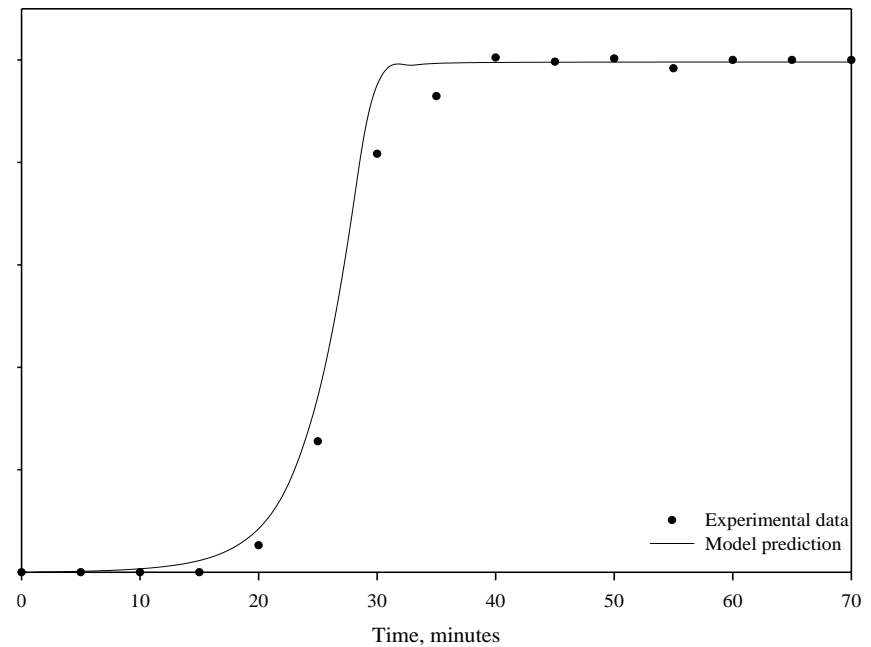
- Solute front sharpens along the bed length
- t_b increases more compared to the increase in t_s

Breakthrough curve analysis

Tapered adsorber with reverse stratified adsorbent



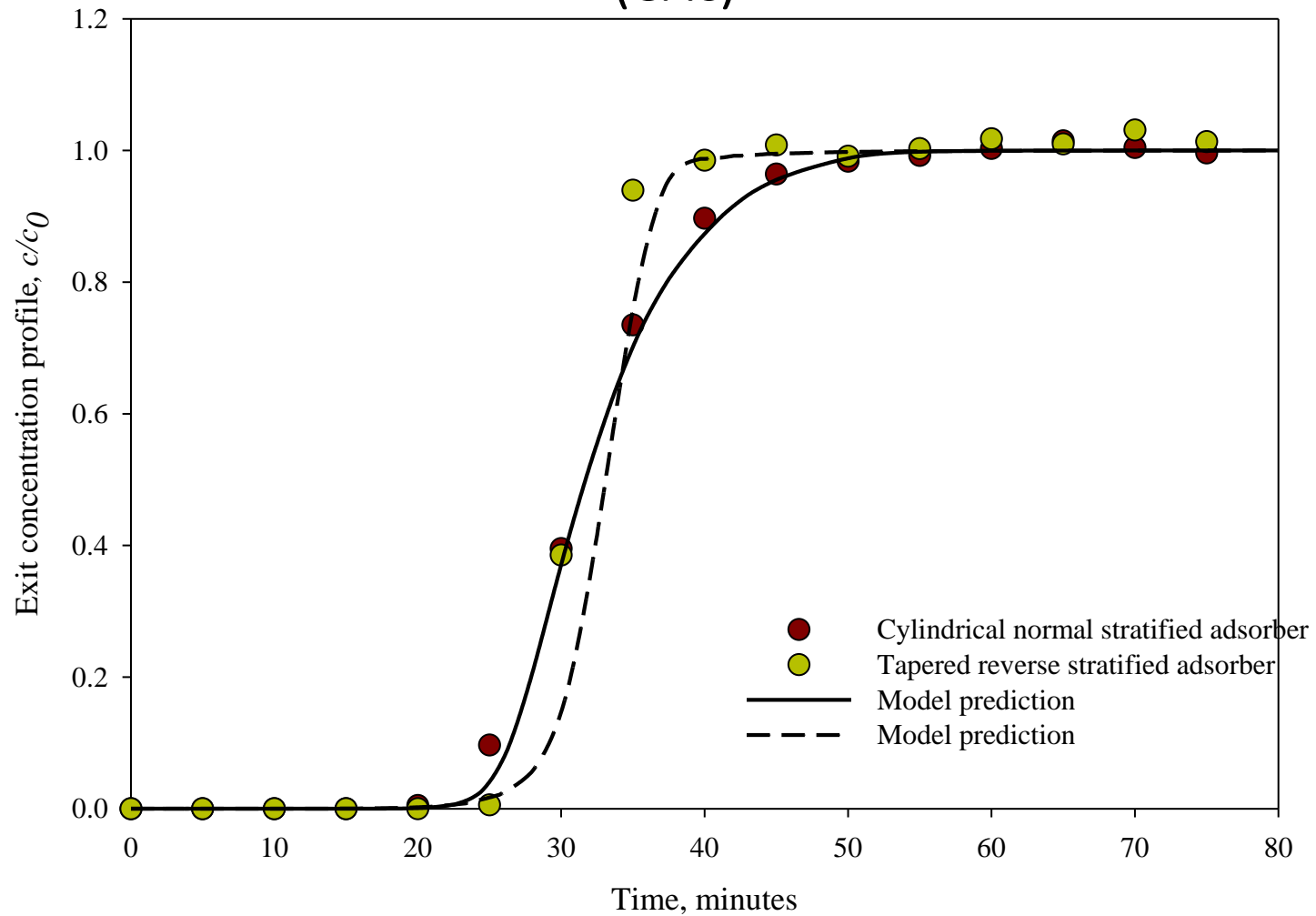
GAC



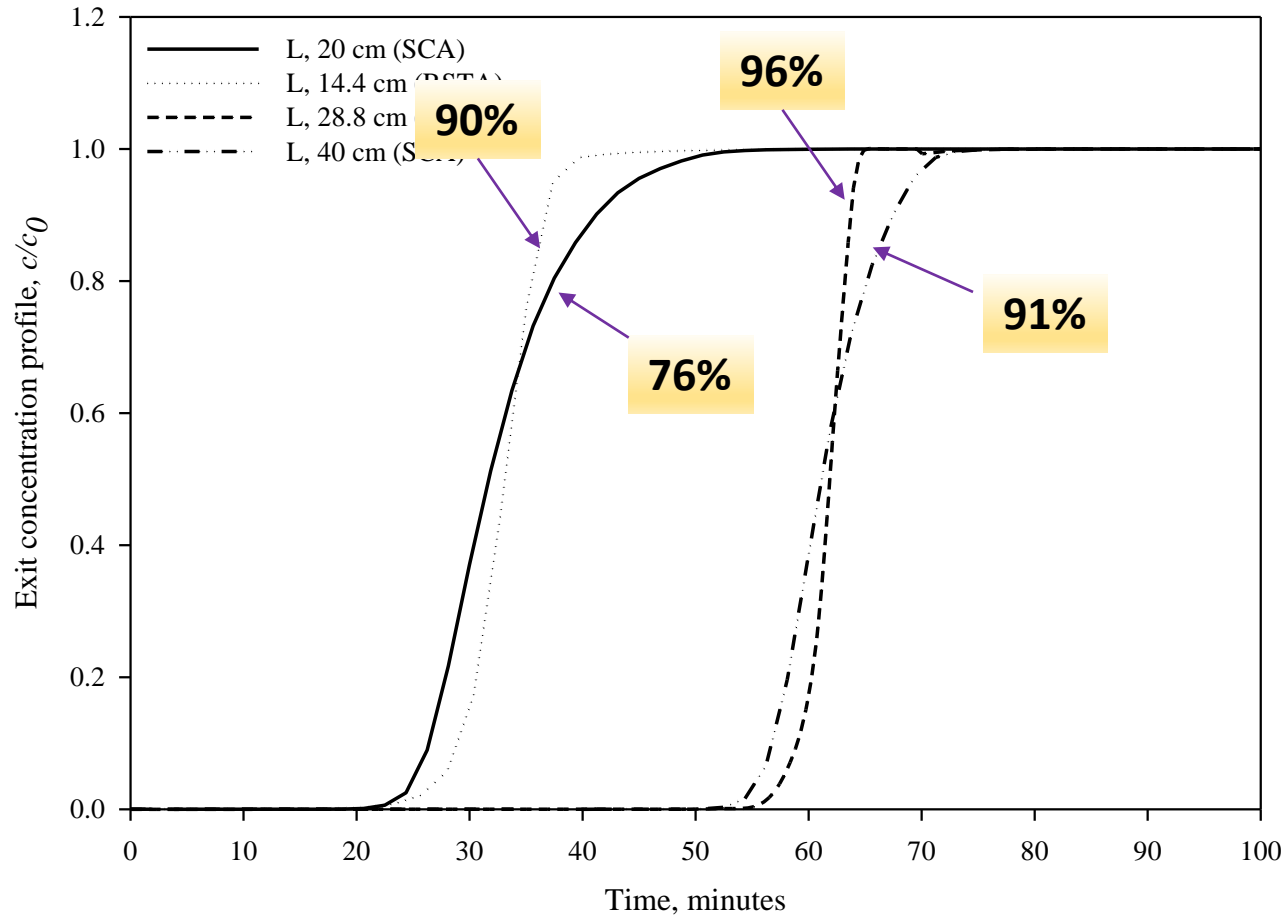
Purolite A835

- Solute front sharpens along the bed length
- Combined effect of decrease in shock front velocity and increase in mass transfer effects

Comparison of exit concentration profiles: Cylindrical adsorber with normal stratified adsorbent and tapered adsorber with reverse stratified adsorbent (GAC)








Comparison of exit concentration profiles: SCA and RSTA with 5 layers of adsorbent particles at double bed length (GAC)



- Double bed length is required for SCA to match the performance of RSTA
- RSTA will require lower adsorbent inventory and reduces the total cost

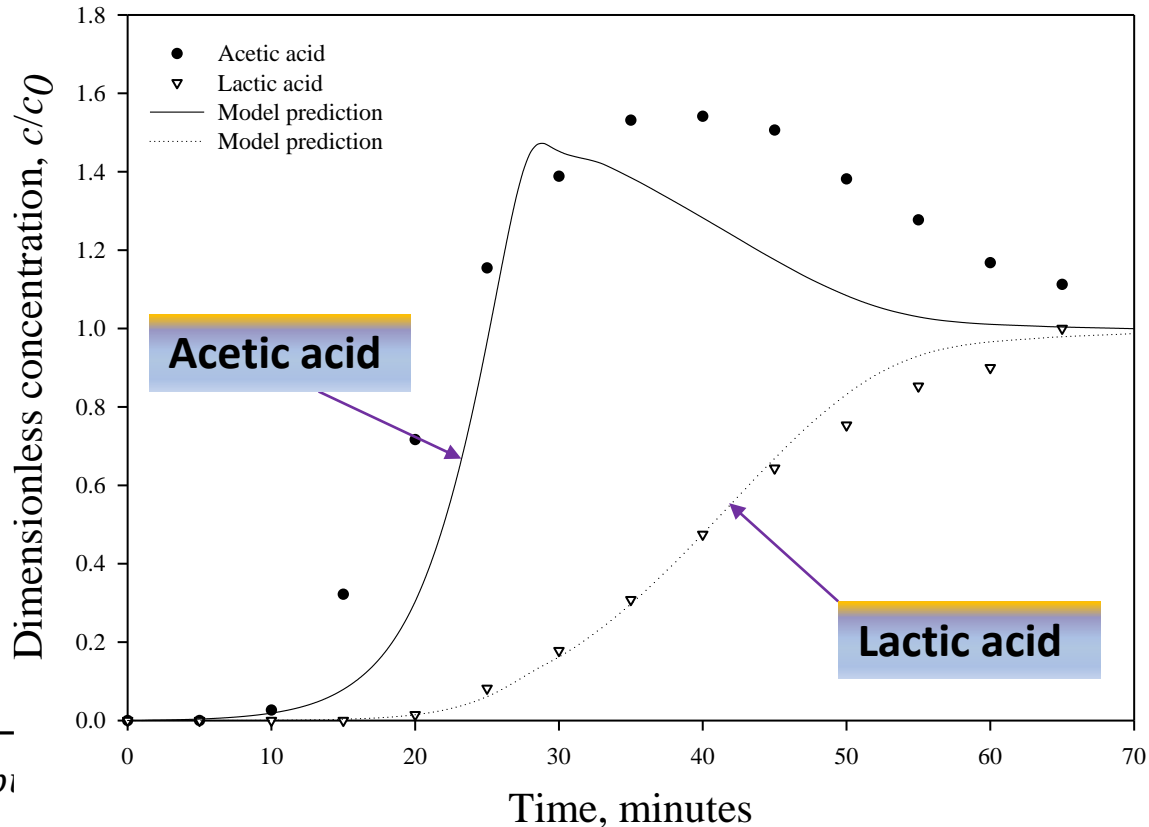
Comparison of shock front velocities and MTZ lengths for various packed bed configurations (GAC)

| Experimental parameters | Cylindrical adsorber - single particle size | Normal stratified cylindrical bed | Reverse stratified cylindrical bed | Reverse stratified tapered bed |
|---|---|---|--|--|
| t_b , min | 24.8 | 23.3 | 27.6 | 26 |
| t_s , min | 39.3 | 42.5 | 43 | 35 |
| t_{MTZ} , min | 14.5 | 19.2 | 15.4 | 9 |
| U_{sh} , cm/min | 0.612 | 0.511 | 0.445 | 0.308 |
| L_{MTZ} , cm | 8.874  | 9.81  | 6.85  | 2.77   |
| <i>Fractional bed capacity utilization</i> | 0.78 | 0.76 | 0.82 | 0.90 |
| <i>Fractional bed capacity utilization at double bed length</i> | | 0.91 | | 0.96 |

Multicomponent adsorption dynamics

Breakthrough profiles for mixed acid: pH 2.8

Lactic acid $C_0 = 15$ g/L, Acetic acid $C_0 = 6$ g/L



$$q_{pi} = \frac{q_{mi} K_i c_{pi}}{1 + \sum_i^k K_i c_{pi}}$$

- Competitive effect of organic acids on Purolite A835 resin
- Roll-over effect occurs and exit concentration of acetic acid is 1.6 times inlet concentration

Conclusion

- The recovery of organic acids from aqueous solutions was modeled using the General Rate Model that considers external and intraparticle diffusion resistances and nonlinear adsorption isotherm
- COMSOL Multiphysics software was found to be an effective tool for process modeling of batch and fixed-bed adsorbers.
- Process modeling of stratified beds was effectively implemented using COMSOL software
- Kinetic parameters estimated from batch studies gave good predictions for the experimental data
- Reverse stratified tapered adsorber shows higher bed capacity utilization compared to other configurations
- COMSOL implementation of multicomponent adsorption dynamics correctly predicted roll over effects of components